

# CMSC 471: Machine Learning

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# Why study learning?

- **Discover** new things or structure previously unknown
  - Examples: data mining, scientific discovery
- Fill in skeletal or **incomplete specifications** in a domain
  - **Large, complex systems** can't be completely built by hand & require dynamic updating to incorporate new info.
  - Learning new characteristics expands the domain or expertise and **lessens the “brittleness” of the system**
- **Acquire models automatically from data** rather than by manual programming
- Build agents that can **adapt** to users, other agents, and their environment
- Understand and improve efficiency of **human learning**

# What does it mean to learn?

Wesley has been taking an AI course

Geordi, the instructor, needs to determine if Wesley has “learned” the topics covered, at the end of the course

What is a “reasonable” exam?

**(Bad) Choice 1:** History of pottery

Wesley’s performance is not indicative of what was learned in AI

**(Bad) Choice 2:** Questions answered during lectures

Open book?

A **good test** should test ability to answer “related” but “new” questions on the exam

Generalization

# Model, parameters and hyperparameters

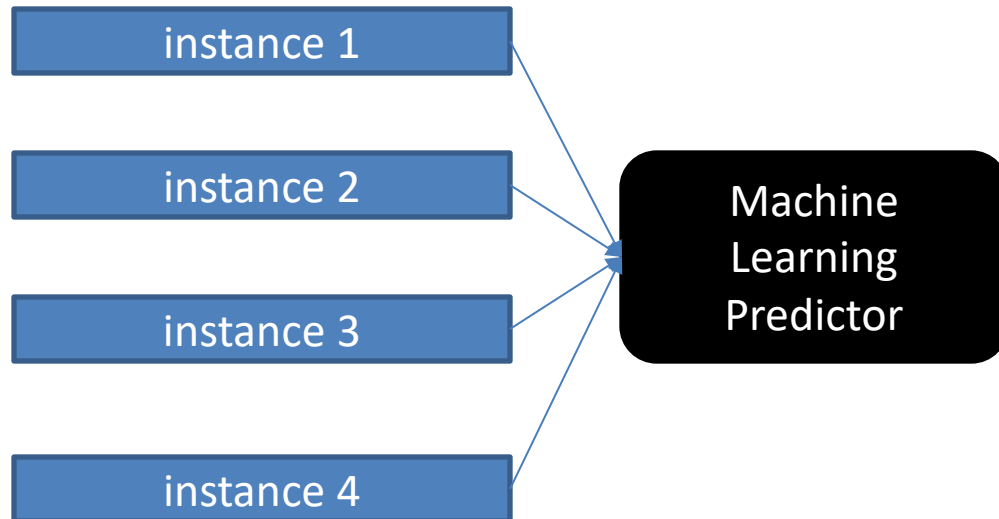
Model: mathematical formulation of system (e.g., classifier)

Parameters: primary “knobs” of the model that are set by a learning algorithm

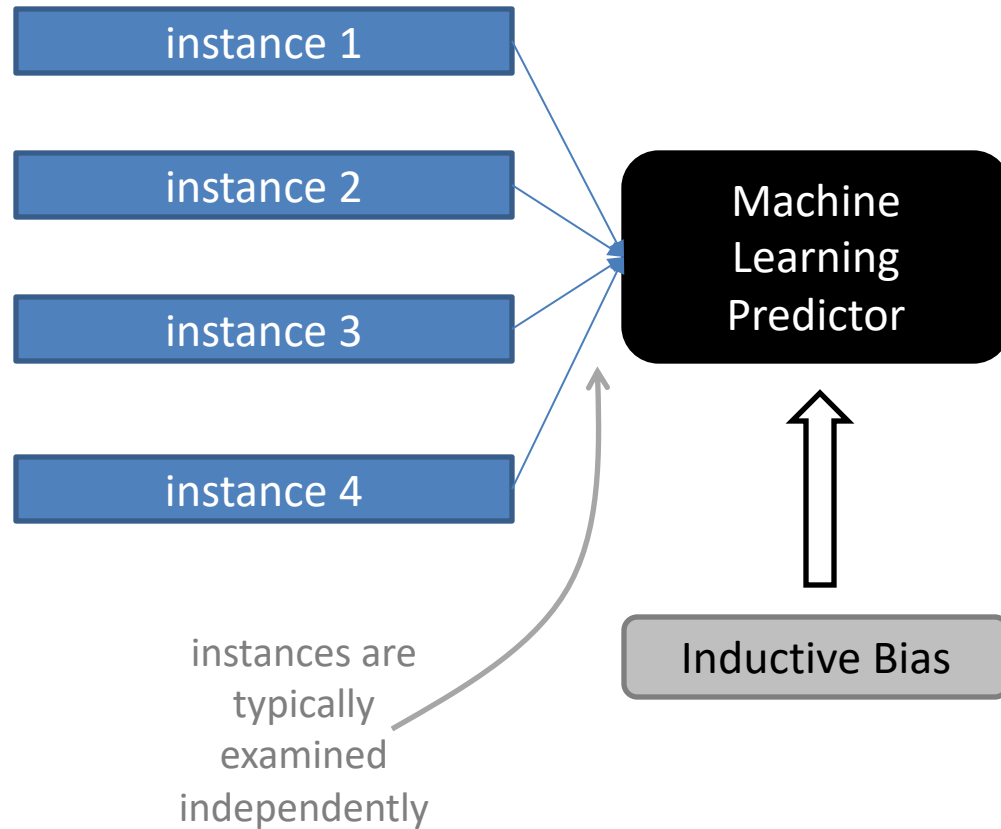


Hyperparameter: secondary “knobs” set by designer

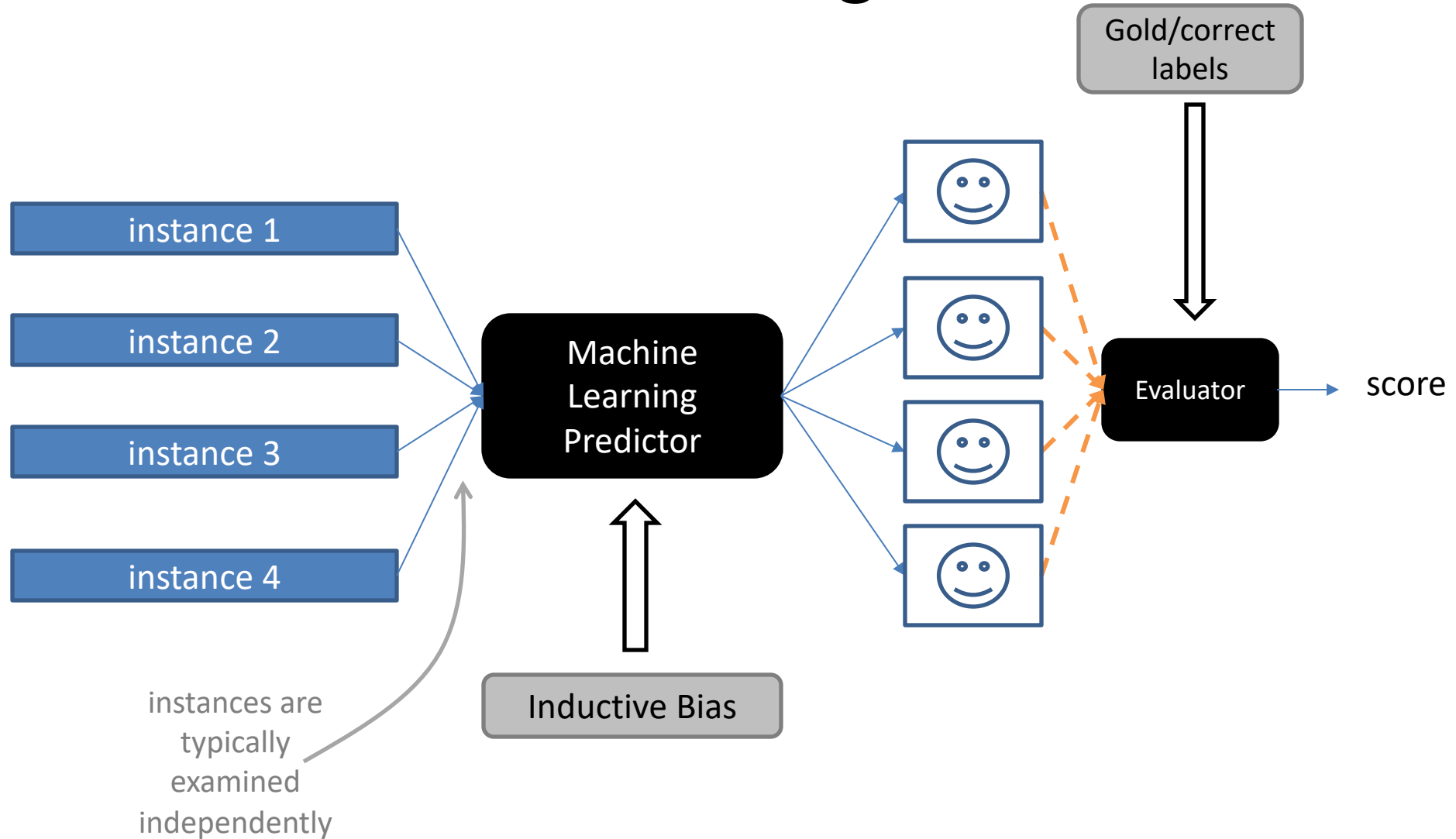
# Machine Learning Framework: Learning



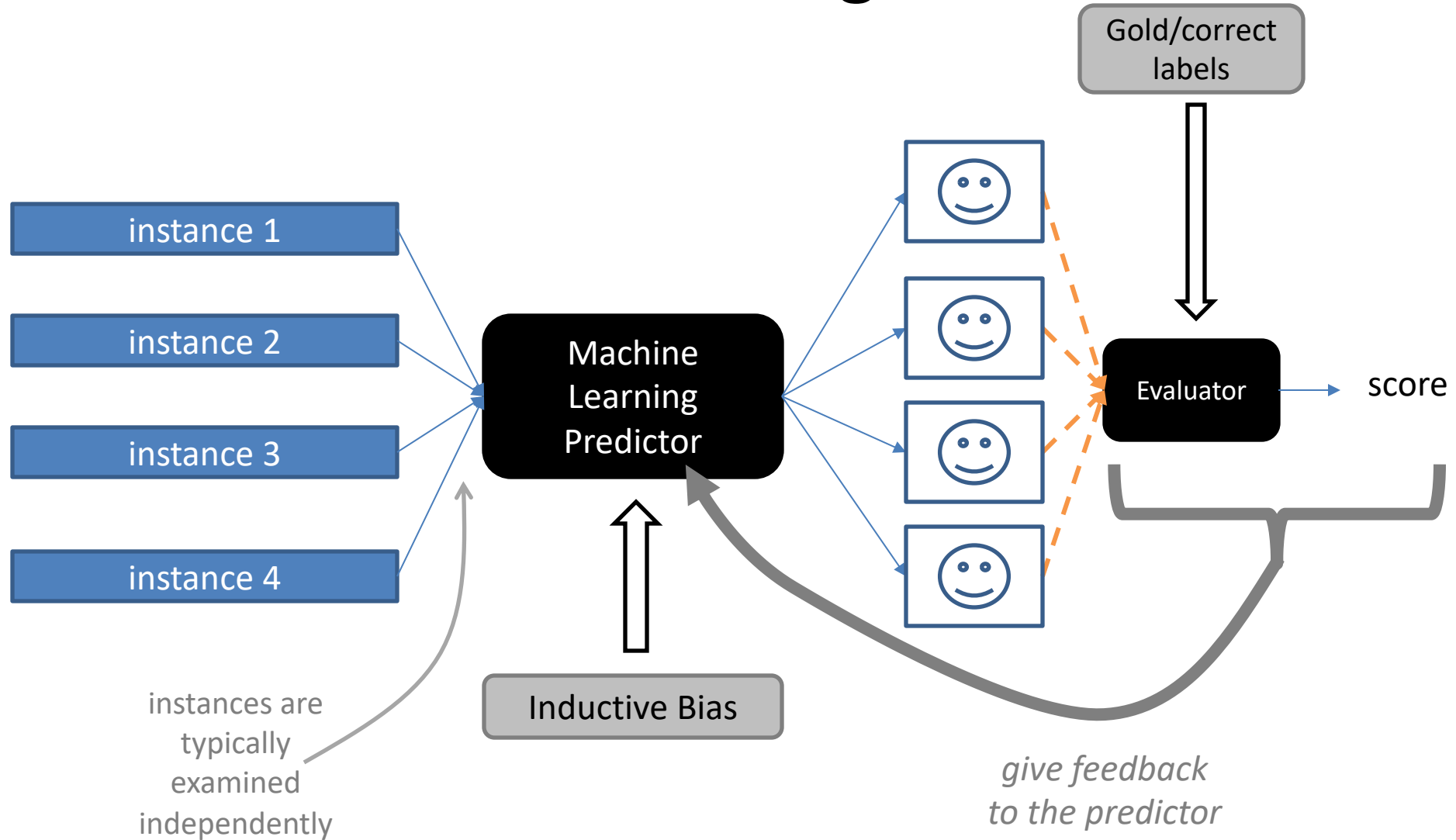
# Machine Learning Framework: Learning



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# Machine Learning Framework: Learning





# Classify with Goodness

predicted label

$$= \underset{\text{label}}{\text{arg max}} \text{score}(\text{example}, \text{label})$$


scoring model

$\text{score}_{\theta}$  (Instance of data ("datum"))



objective

$F(\theta)$

*(implicitly) dependent on the  
observed data  $X =$  *

# ML Framework Example

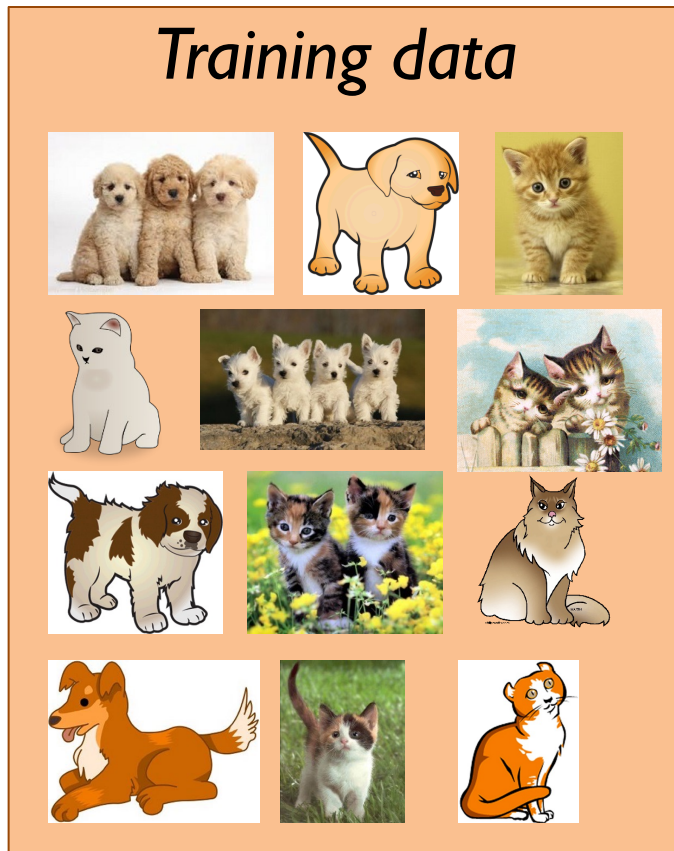
## Puppy classifier

*Training data*



# ML Framework Example

Puppy classifier



Classifier  
(trained  
**model**)

# ML Framework Example

## Puppy classifier

*Training data*

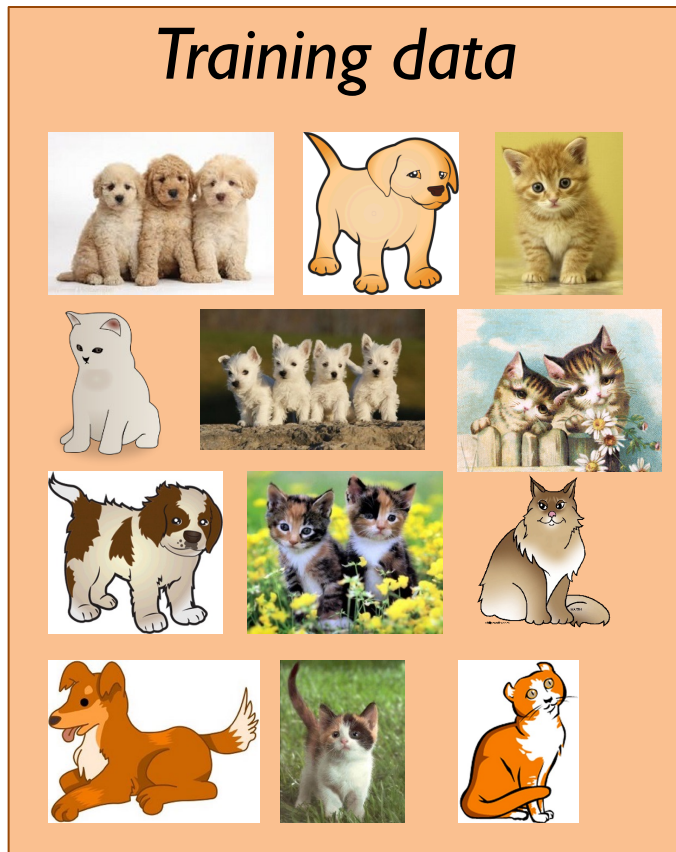


Classifier  
(trained  
**model**)

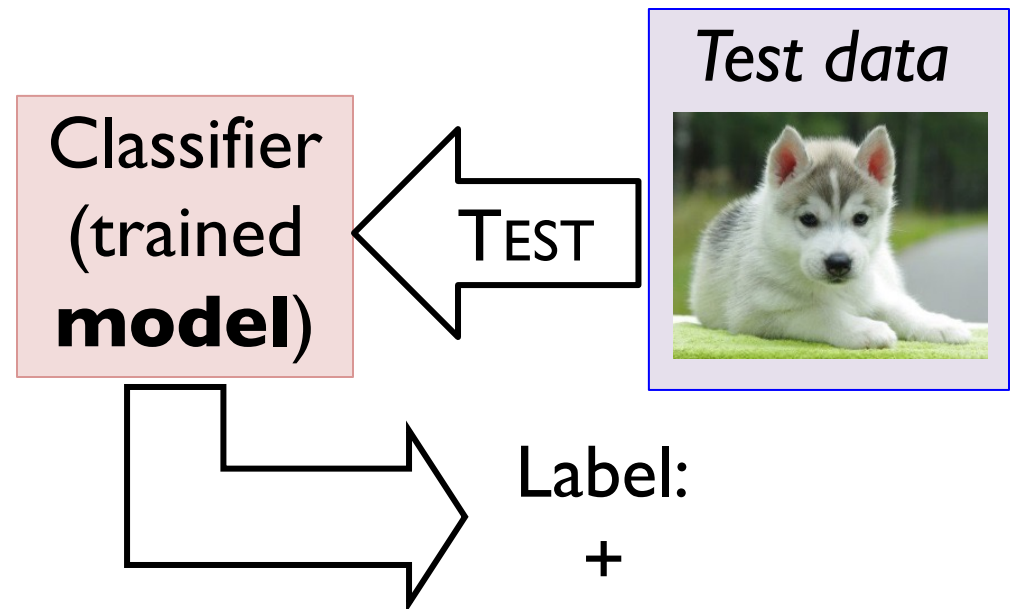
*Test data*



# ML Framework Example



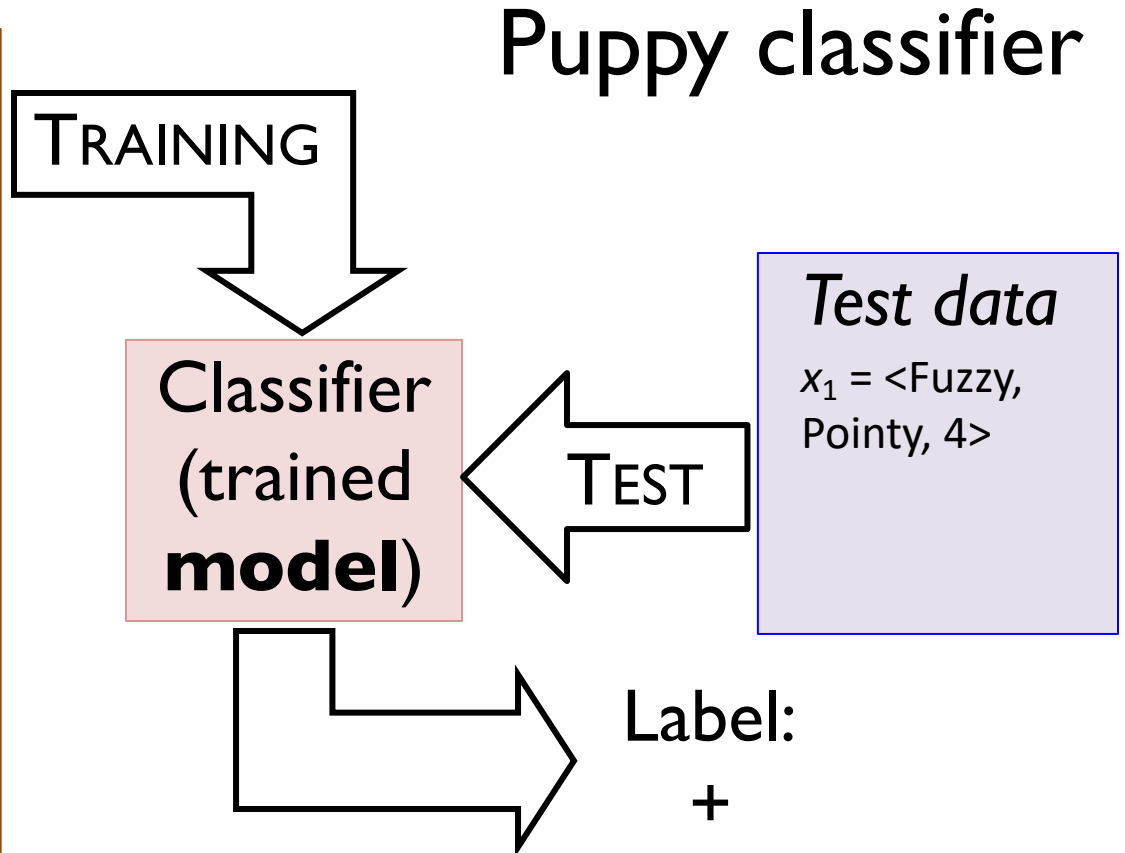
## Puppy classifier



# ML Framework Example

*Training data, X*

<i>Text-ure</i>	<i>Ears</i>	<i>Legs</i>	<i>Class</i>
Fuzzy	Round	4	+
Slimy	Missing	8	-
Fuzzy	Pointy	4	-
Fuzzy	Round	4	+
Fuzzy	Pointy	4	+
...			



# The Big Idea and Terminology

Given some data, learn a model of how the world works that lets you predict new data

- **Training Set:** Data from which you learn initially
- **Model:** What you learn; a “model” of how inputs are associated with outputs
- **Test set:** New data you test your model against
- **Corpus:** A body of text data (pl.: corpora)
- **Representation:** The computational expression of data

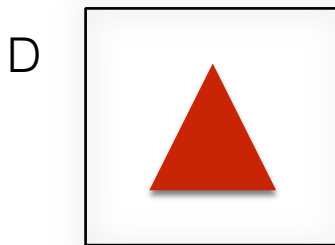
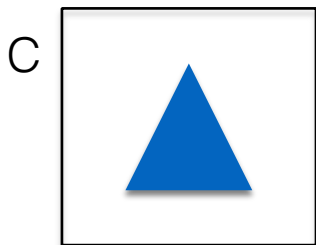
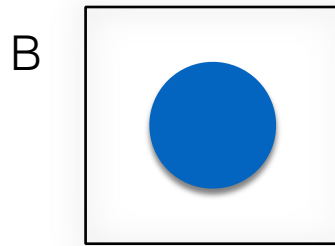
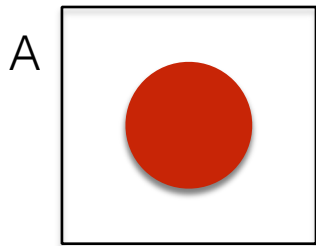


# General ML Consideration: Inductive Bias

What do we know *before* we see the data, and how does that influence our modeling decisions?

# General ML Consideration: Inductive Bias

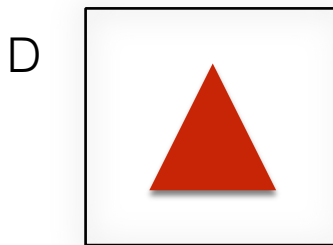
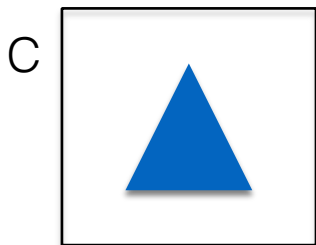
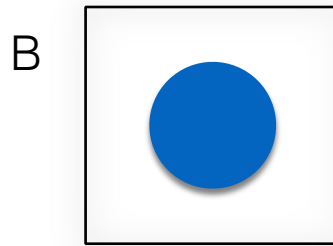
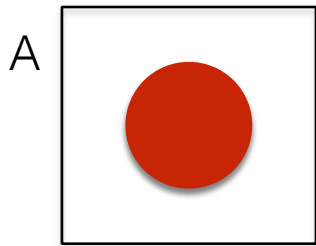
What do we know *before* we see the data, and how does that influence our modeling decisions?



*Partition these into two groups...*

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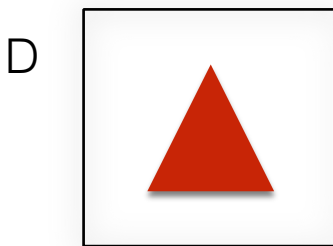
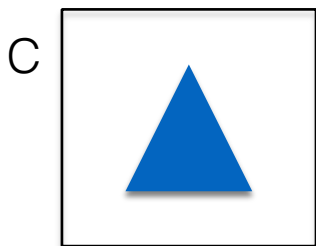
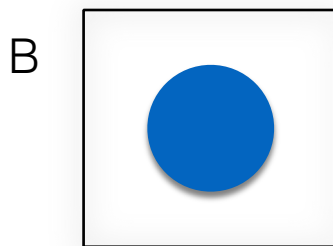
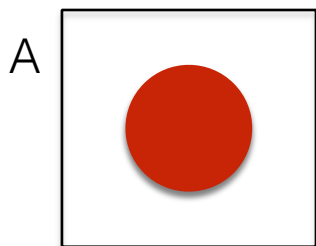


*Partition these into two groups*

*Who selected **red** vs. **blue**?*

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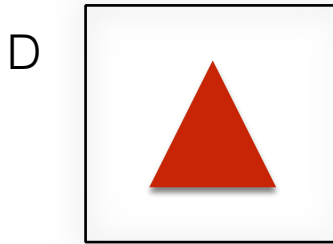
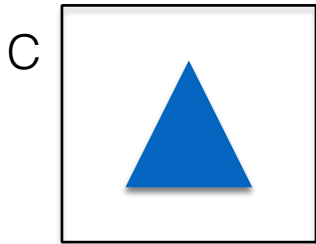
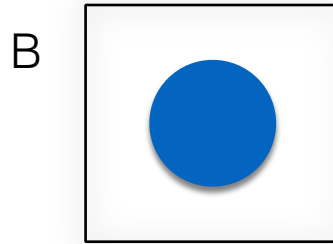
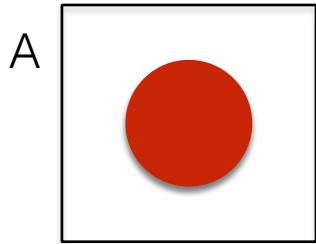
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*Who selected **red** vs. **blue**?*

*Who selected  vs.  ?*

# General ML Consideration: Inductive Bias

What do we know *before* we see the data, and how does that influence our modeling decisions?



*Partition these into two groups*

*Who selected **red** vs. **blue**?*

*Who selected  vs.  ?*

Tip: Remember how your own  
biases/interpretation are influencing your  
approach

# AI & ML

# AI and Learning Today

- 50s&60s: neural network learning popular

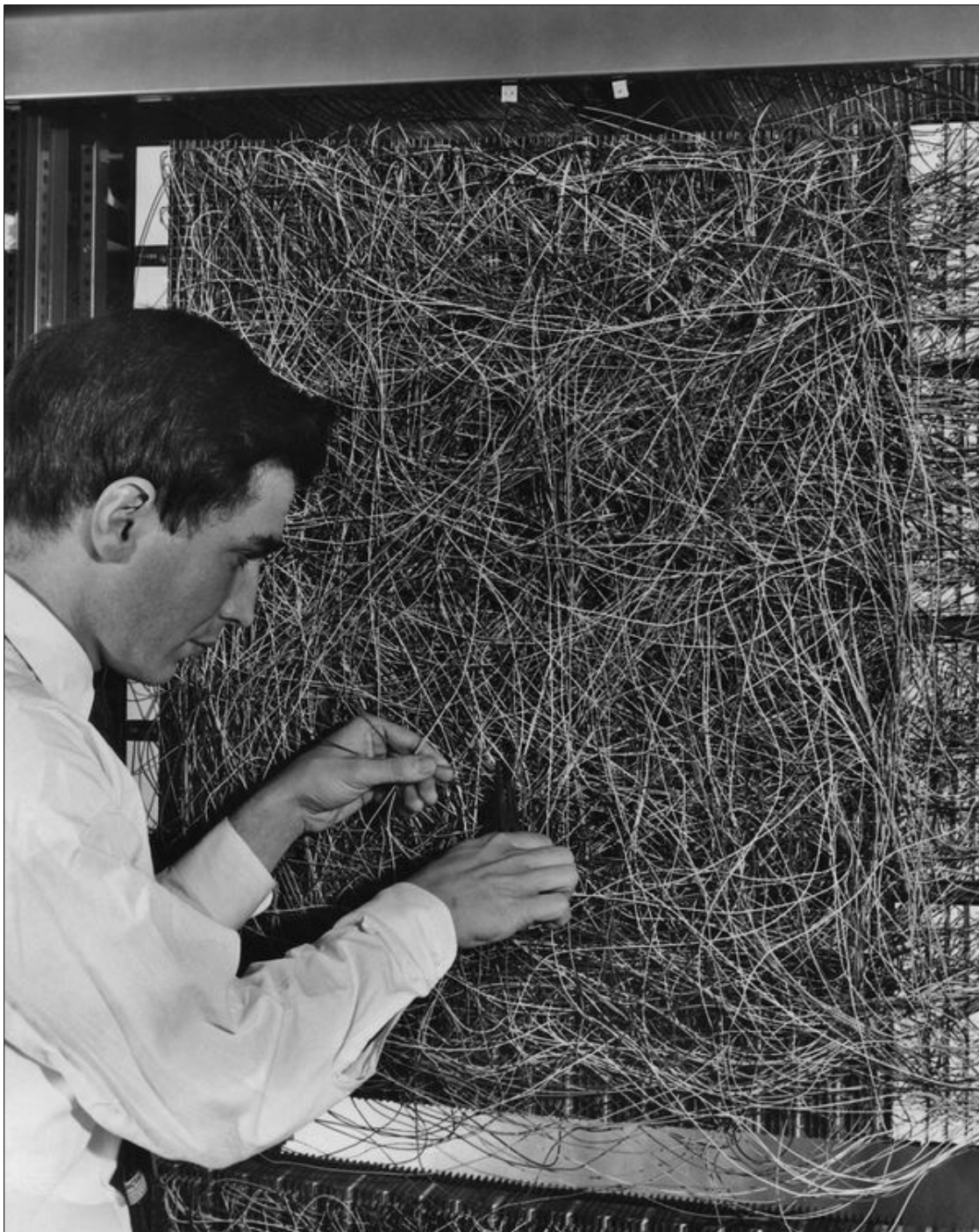
Marvin Minsky did neural networks for his dissertation

- Mid 60s: replaced by paradigm of manually encoding & using symbolic knowledge

Cf. [Perceptrons](#), Minsky & Papert book showed limitations of perceptron model of neural networks

- 90s: more data & Web drove interest in statistical machine learning techniques & data mining
- Now: machine learning techniques & big data play biggest driver in almost all successful AI systems  
... and neural networks are the current favorite approach

# Neural Networks 1960



A man adjusting the random wiring network between the light sensors and association unit of scientist Frank Rosenblatt's Perceptron, or MARK 1 computer, at the Cornell Aeronautical Laboratory, Buffalo, New York, circa 1960. The machine is designed to use a type of artificial neural network, known as a perceptron.



# Machine Learning Successes

- Games: chess, go, poker
- Text sentiment analysis
- Email spam detection
- Recommender systems (e.g., Netflix, Amazon)
- Machine translation
- Speech understanding
- SIRI, Alexa, Google Assistant, ...
- Autonomous vehicles
- Individual face recognition
- Understanding digital images
- Credit card fraud detection
- Showing annoying ads



# Major Machine learning paradigms (1)

- **Rote:** 1-1 mapping from inputs to stored representation, learning by memorization, association-based storage & retrieval
- **Induction:** Use specific examples to reach general conclusions
- **Clustering:** Unsupervised discovery of natural groups in data

# Major Machine learning paradigms (2)

- **Analogy:** Find correspondence between different representations
- **Discovery:** Unsupervised, specific goal not given
- **Genetic algorithms:** *Evolutionary* search techniques, based on *survival of the fittest*
- **Reinforcement:** Feedback (positive or negative reward) given at the end of a sequence of steps
- **Deep learning:** *artificial neural networks* with *representation learning* for ML tasks

# **TYPES OF LEARNING**

# Three Axes for Thinking About Your ML Problem

Classification

Regression

Clustering

Fully-supervised

Semi-supervised

Un-supervised

Probabilistic

Neural

Generative

Memory-based

Conditional

Exemplar

Spectral

...

*the **task**: what kind of problem are you solving?*

*the **data**: amount of human input/number of labeled examples*

*the **approach**: how any data are being used*

# Types of learning problems

- **Supervised:** learn from training examples
  - Regression:
  - Classification: Decision Trees, SVM
- **Unsupervised:** learn w/o training examples
  - Clustering
  - Dimensionality reduction
  - Word embeddings
- **Reinforcement learning:** improve performance using feedback from actions taken
- **Lots more we won't cover**
  - Hidden Markov models, Learning to rank, Semi-supervised learning, Active learning ...

# Machine Learning Problems

*Supervised Learning*

*Unsupervised Learning*

*Discrete*

classification or  
categorization

clustering

*Continuous*

regression

dimensionality  
reduction

# Inductive Learning Framework

- Raw input data from sensors or a database preprocessed to obtain **feature vector**,  $\mathbf{X}$ , of **relevant** features for classifying examples
- Each  $\mathbf{X}$  is a list of (attribute, value) pairs
- $n$  attributes (a.k.a. features): fixed, positive, and finite
- Features have fixed, finite number # of possible values
  - Or continuous within some well-defined space, e.g., “age”
- Each example is a point in an  $n$ -dimensional feature space
  - $X = [\text{Person:Sue, EyeColor:Brown, Age:Young, Sex:Female}]$
  - $X = [\text{Cheese:}f, \text{Sauce:}t, \text{Bread:}t]$
  - $X = [\text{Texture:Fuzzy, Ears:Pointy, Purrs:Yes, Legs:4}]$



# **SUPERVISED LEARNING**

# Supervised learning

- Given training examples of inputs & corresponding outputs, produce “correct” outputs for new inputs
- Two important scenarios:
  - **Classification:** outputs typically labels (goodRisk, badRisk); learn decision boundary to separate classes
  - **Regression:** aka *curve fitting* or *function approximation*; Learn a *continuous* input-output mapping from examples, e.g., for a zip code, predict house sale price given its square footage

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# Classification Examples

Assigning subject  
categories, topics, or  
genres

Spam detection

Authorship identification

Age/gender identification

Language Identification

Sentiment analysis

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*Input:*

an instance

a fixed set of classes  $C = \{c_1, c_2, \dots, c_J\}$

*Output:* a predicted class  $c$  from  $C$

# Classification: Hand-coded Rules?

Assigning subject categories, topics, or genres

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...

Rules based on combinations of words or other features  
spam: black-list-address OR (“dollars” AND “have been selected”)

Accuracy can be high  
If rules carefully refined by expert

Building and maintaining these rules is expensive

Can humans faithfully assign uncertainty?

# Classification:

## Supervised Machine Learning

Assigning subject categories, topics, or genres

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...

### *Input:*

an instance  $d$

a fixed set of classes  $C = \{c_1, c_2, \dots, c_j\}$

A training set of  $m$  hand-labeled instances  $(d_1, c_1), \dots, (d_m, c_m)$

### *Output:*

a learned classifier  $\gamma$  that maps instances to classes

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$\gamma$  learns to associate certain *features* of instances with their labels



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Naïve Bayes  
Logistic regression  
Support-vector machines  
k-Nearest Neighbors

...

# Classification Example: Face Recognition

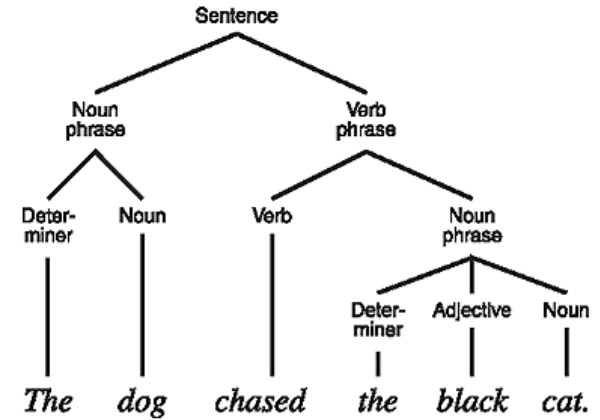
Class	Image	Class	Image
Avrim		Tom	
Avrim		Tom	
Avrim		Tom	
Avrim		Tom	

What is a good *representation* for images?

Pixel values? Edges?

# Classification Example: Sequence & Structured Prediction

Google Translate interface showing a Hindi sentence and its English translation. The Hindi text discusses a cricket match in Australia. The English translation is: "Being played in Australia tri-series one-day international cricket match can be a Sunday Super Sunday. Australia and India will face each host in Melbourne. The first match Australia beat England by three wickets with a superb debut of bonus points. The hands of the one-day series in India before Australia lost 0-2 in the four-Test series. After the end of the third Test draw India captain Mahendra Singh Dhoni was also announced his retirement from Test cricket. Now is not the right day of Test cricket whites Dhoni color jersey will be anxious to show his usual self."



# Ingredients for classification

Inject *your* knowledge into a learning system

*Feature representation*

*Training data:  
labeled examples*

*Model*

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Problem specific

Difficult to learn from bad  
ones

*Feature representation*

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Labeling data == \$\$\$

Sometimes data is available for “free”

*Feature representation*

*Training data:  
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Difficult to learn from bad ones

*Feature representation*

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*Training data:  
labeled examples*

No single learning algorithm is always good (“no free lunch”)

Different learning algorithms work differently

*Model*

# Regression

Like classification, but real-valued



# Regression Example: Stock Market Prediction

## S&P 500

S&P Indices: .INX - Jan 16 4:30 PM ET

**2,019.42** ↑26.75 (1.34%)

1 day

5 day

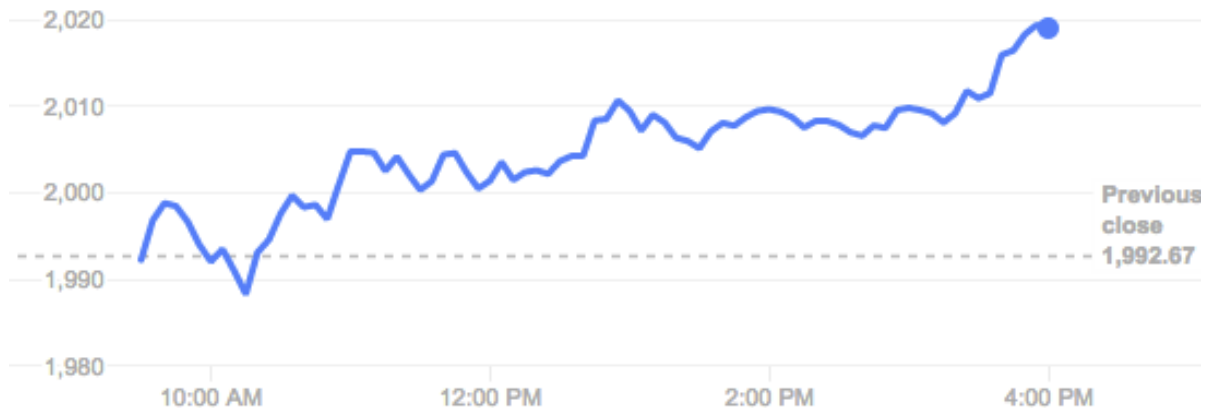
1 month

3 month

1 year

5 year

max



Open 1,992.25  
High 2,020.46  
Low 1,988.12

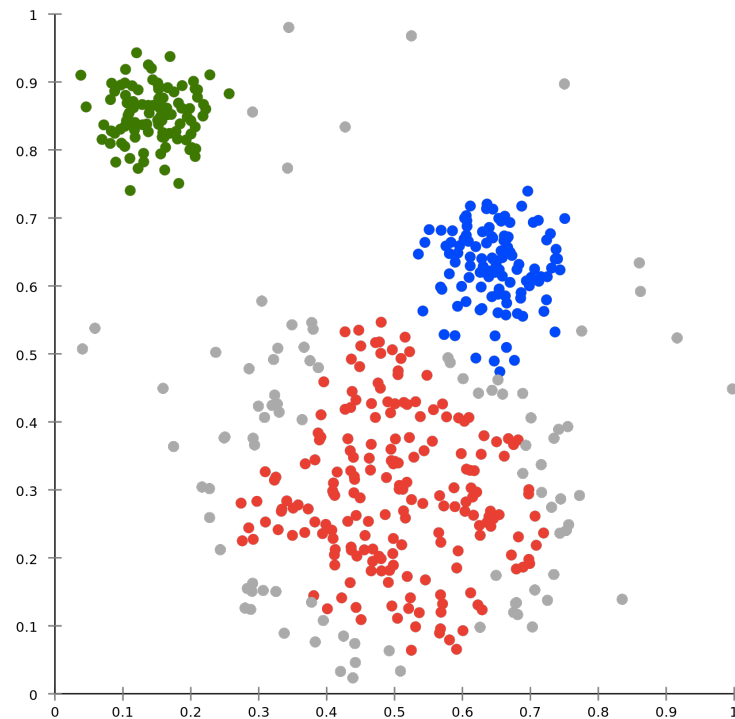
Market cap -  
P/E ratio (ttm) -  
Dividend yield -

# Unsupervised Learning

Given only *unlabeled* data as input, learn some sort of structure, e.g.:

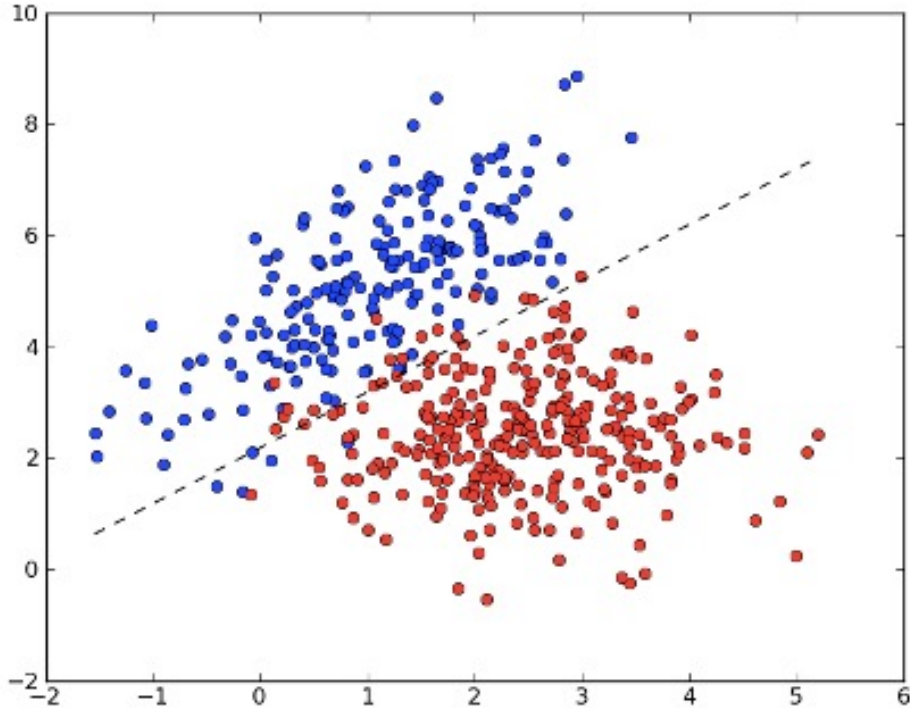
- **Clustering**: group Facebook friends based on similarity of post texts and friends
- **Embeddings**: Find sets of words whose meanings are related (e.g., doctor, hospital)
- **Topic modelling**: Induce N topics and words most common in documents about each

# Unsupervised learning: Clustering



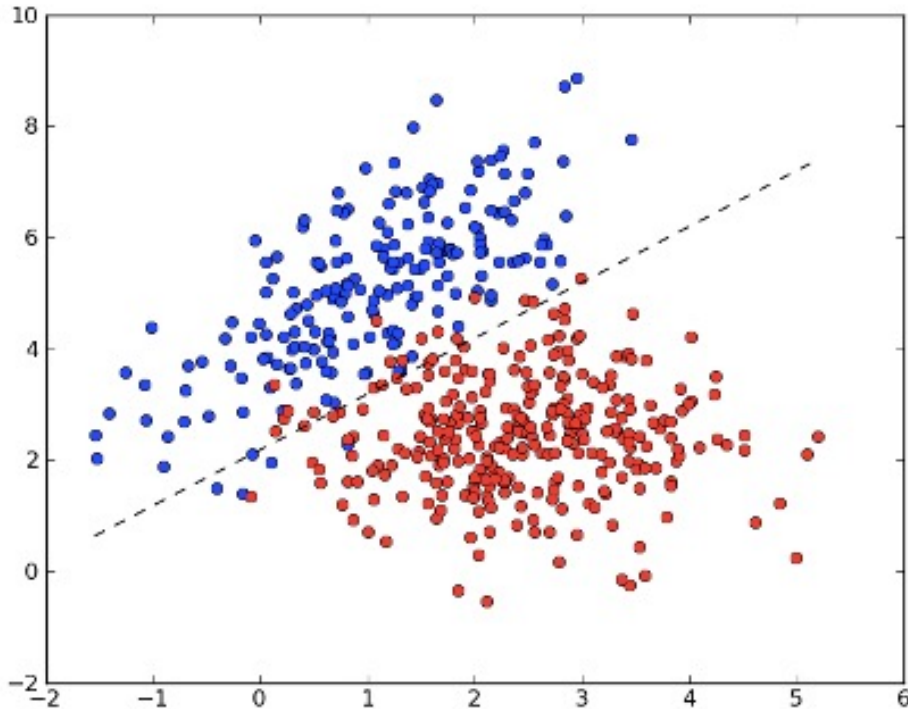
# LINEAR MODELS

# Linear Models



- Can be used for either regression or classification
- A number of instances for classification. Common ones are:
  - Perceptron
  - Linear SVM
  - Logistic regression
    - (yes, even though “regression” is in the name 😊)

# Linear Models: Core Idea

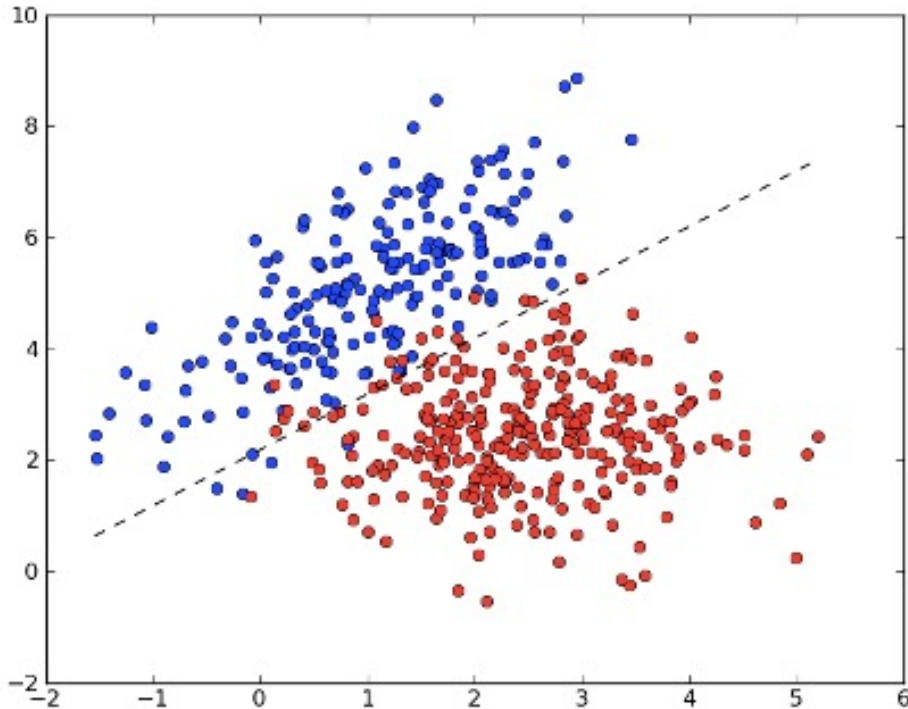


Model the relationship between the input data  $X$  and corresponding labels  $Y$  via a linear relationship (non-zero intercepts  $b$  are okay)

$$Y = W^T X + b$$

Items to learn:  $W, b$

# Linear Models: Core Idea



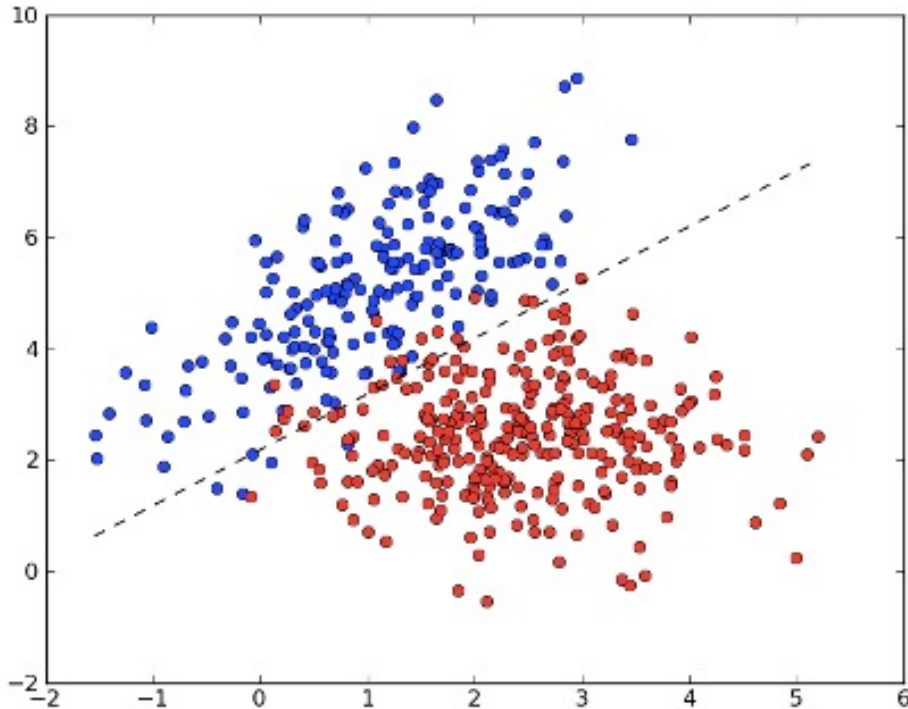
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Items to learn:  $W, b$

For regression: the output of this equation *is* the predicted value

For classification: one class is on one side of this line, the other class is on the other



# Linear Models in sklearn

## 1.1. Linear Models

1.1.1. Ordinary Least Squares

1.1.2. Ridge regression and  
classification

1.1.3. Lasso

1.1.4. Multi-task Lasso

1.1.5. Elastic-Net

1.1.6. Multi-task Elastic-Net

1.1.7. Least Angle Regression

1.1.8. LARS Lasso

1.1.9. Orthogonal Matching Pursuit  
(OMP)

1.1.10. Bayesian Regression

1.1.11. Logistic regression

1.1.12. Generalized Linear  
Regression

1.1.13. Stochastic Gradient Descent  
- SGD

1.1.14. Perceptron

1.1.15. Passive Aggressive  
Algorithms

1.1.16. Robustness regression:  
outliers and modeling errors

1.1.17. Polynomial regression:  
extending linear models with basis  
functions

These all have easy-to-use interfaces, with the same core interface:

- Training:

*model.fit(X = training\_features,  
y = training\_labels)*

- Prediction:

*model.predict(X = eval\_features)*

# Linear Models in pytorch

Docs > torch.nn > Linear

## LINEAR

**CLASS** `torch.nn.Linear(in_features, out_features, bias=True)`

Applies a linear transformation to the incoming data:  $y = xA^T + b$

This module supports `TensorFloat32`.

### Variables

- **-Linear.weight** – the learnable weights of the module of shape `(out_features, in_features)`. The values are initialized from  $\mathcal{U}(-\sqrt{k}, \sqrt{k})$ , where  $k = \frac{1}{\text{in\_features}}$
- **-Linear.bias** – the learnable bias of the module of shape `(out_features)`. If `bias` is `True`, the values are initialized from  $\mathcal{U}(-\sqrt{k}, \sqrt{k})$  where  $k = \frac{1}{\text{in\_features}}$

Examples:

```
>>> m = nn.Linear(20, 30)
>>> input = torch.randn(128, 20)
>>> output = m(input)
>>> print(output.size())
torch.Size([128, 30])
```

These are “building blocks” not full models.

# A Simple Linear Model

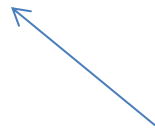
Take CMSC 478 (or 678), or independent study to learn about this in more detail!

predict  $y_i$  from  $\mathbf{x}_i$

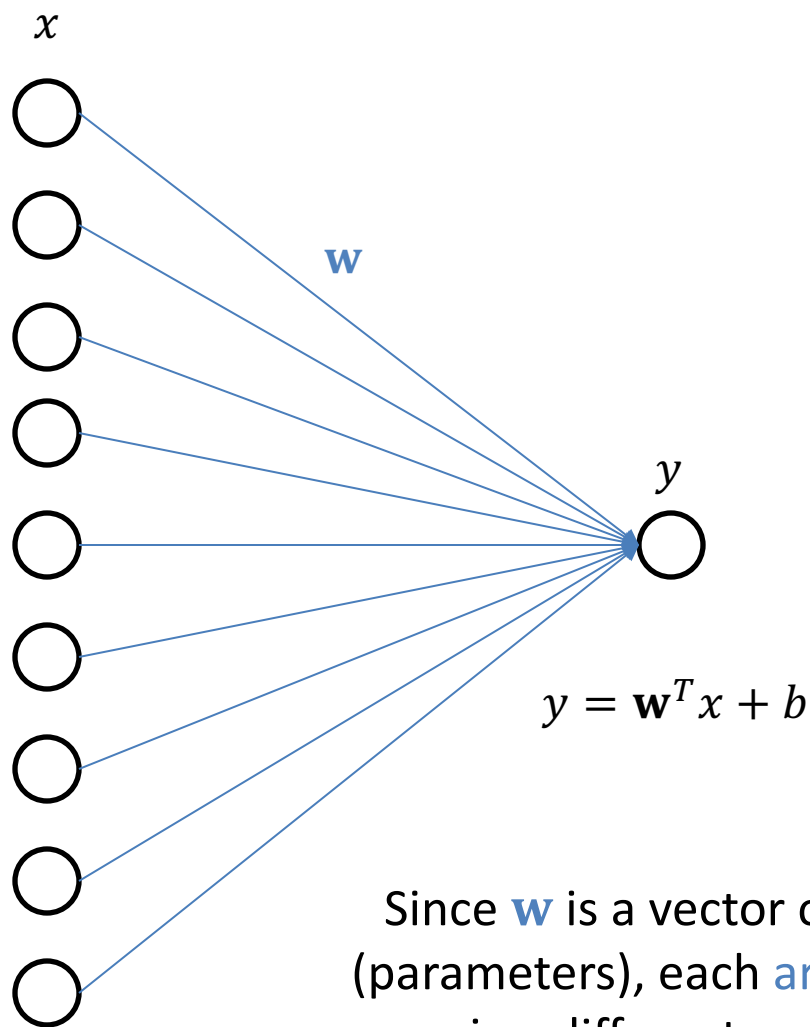
value  $y_i$



data point  $\mathbf{x}_i$ , as a vector of features



# A Graphical View of Linear Models



Since  $\mathbf{w}$  is a vector of weights (parameters), each **arc** from  $x$  to  $y$  is a different parameter

# A Simple Linear Model for Regression

vector  $w$  of weights

$$y_i = \mathbf{w}^T \mathbf{x}_i$$

value  $y_i$

data point  $x_i$ , as a vector of features

The diagram illustrates the equation  $y_i = \mathbf{w}^T \mathbf{x}_i$ . Three blue arrows point from descriptive text to the equation: one from 'vector w of weights' to the  $\mathbf{w}$  term, one from 'value  $y_i$ ' to the  $y_i$  term, and one from 'data point  $x_i$ , as a vector of features' to the  $\mathbf{x}_i$  term.

# A Simple Linear Model for Regression

The diagram shows the equation  $y_i = \mathbf{w}^T \mathbf{x}_i + b$  centered on the page. Four blue arrows point from descriptive text labels to the corresponding parts of the equation: one from 'value  $y_i$ ' to  $y_i$ , one from 'vector  $w$  of weights' to  $\mathbf{w}$ , one from 'data point  $x_i$ , as a vector of features' to  $\mathbf{x}_i$ , and one from 'bias  $b$ ' to  $b$ .

$$y_i = \mathbf{w}^T \mathbf{x}_i + b$$

value  $y_i$

vector  $w$  of weights

data point  $x_i$ , as a vector of features

bias  $b$

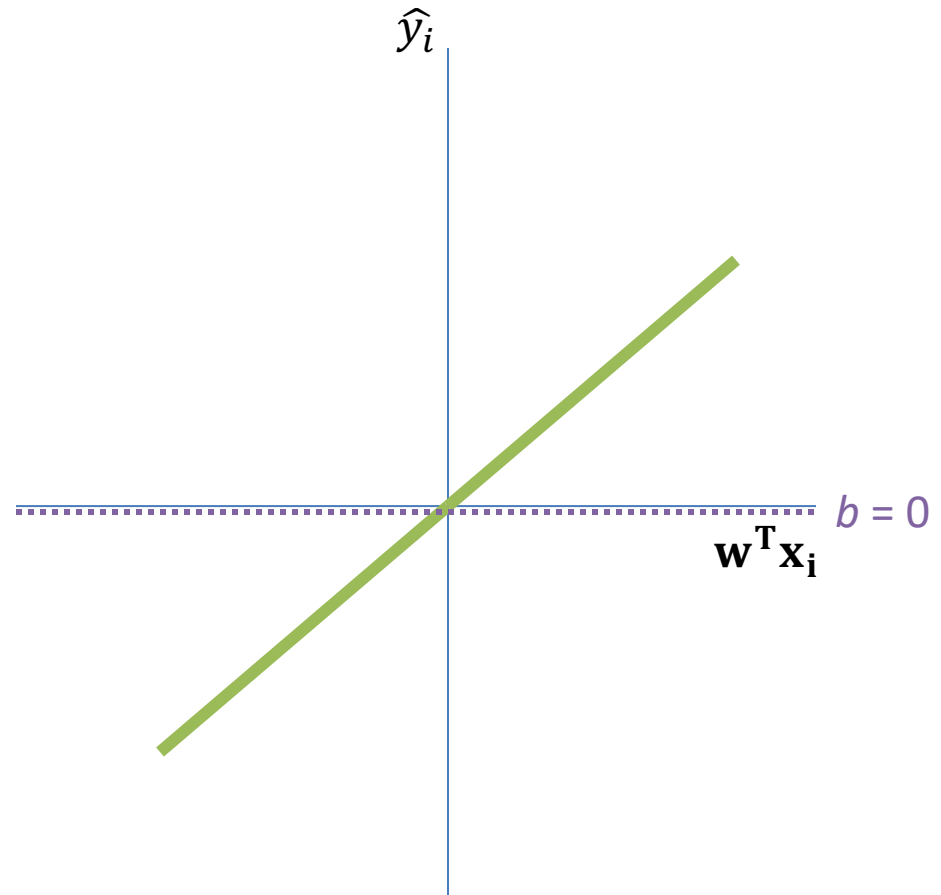
# A Simple Linear Model for Regression

vector  $w$  of weights

$$y_i = \mathbf{w}^T \mathbf{x}_i + 0$$

value  $y_i$

data point  $x_i$ , as a vector of features



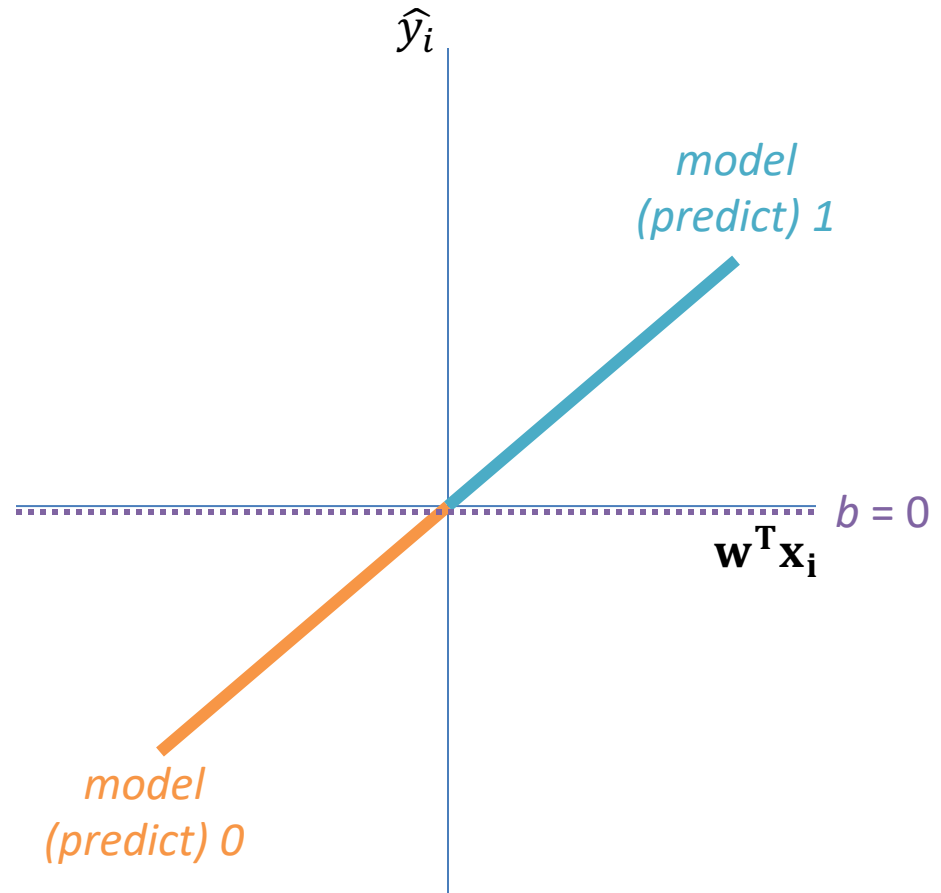
# A Simple Linear Model for Classification

vector  $w$  of weights

$$y_i = \mathbf{w}^T \mathbf{x}_i$$

label  $y_i$   
(binary  $\{0, 1\}$   
value)

data point  $x_i$ , as a  
vector of features





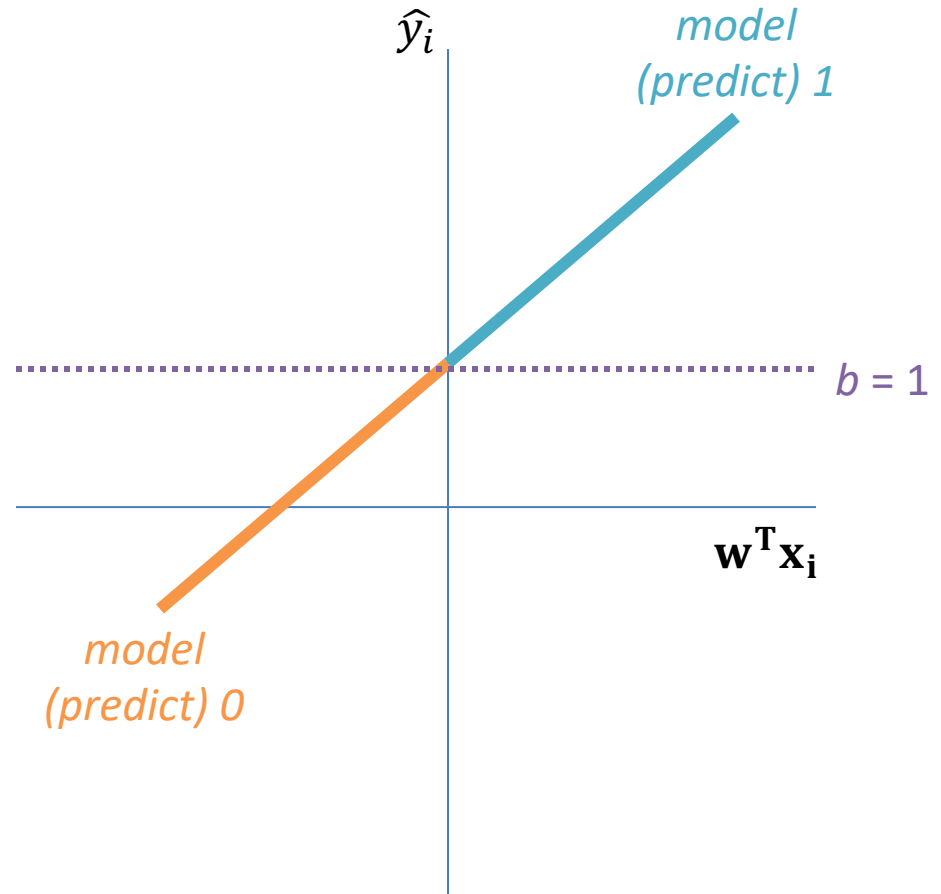
# A Simple Linear Model for Classification

vector  $w$  of weights

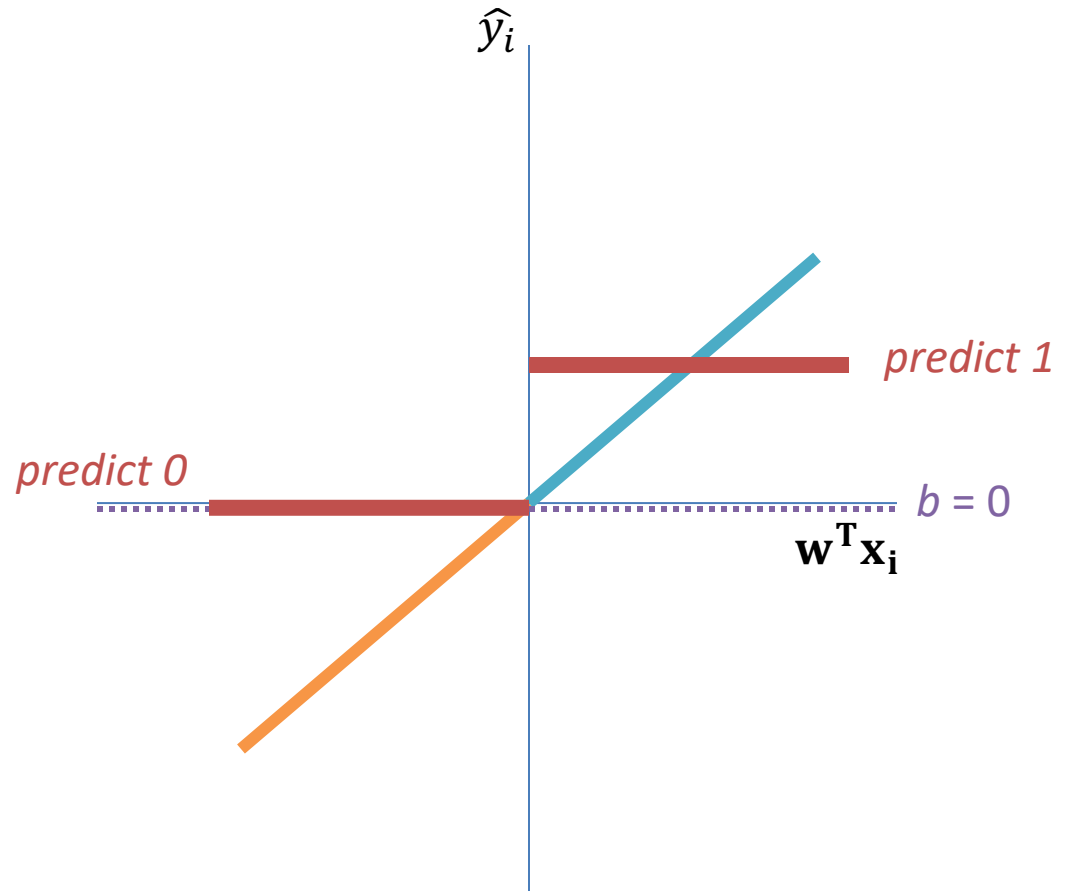
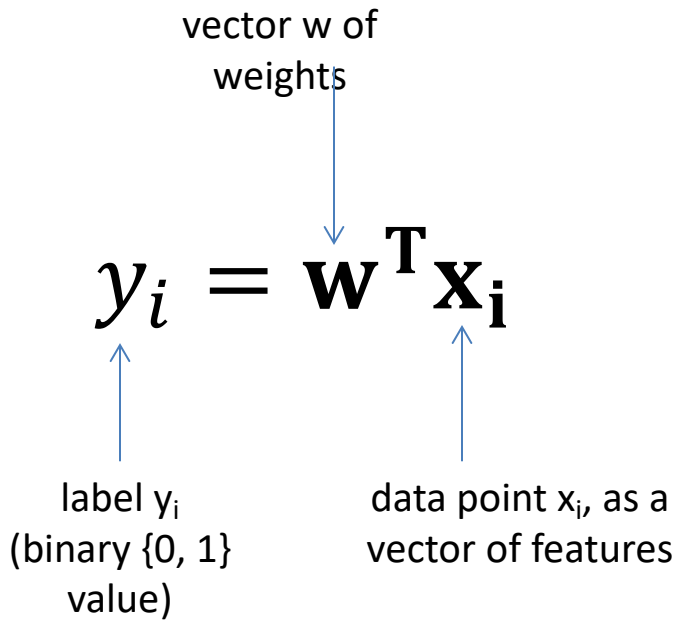
$$y_i = \mathbf{w}^T \mathbf{x}_i + 1$$

label  $y_i$   
(binary  $\{0, 1\}$   
value)

data point  $x_i$ , as a  
vector of features

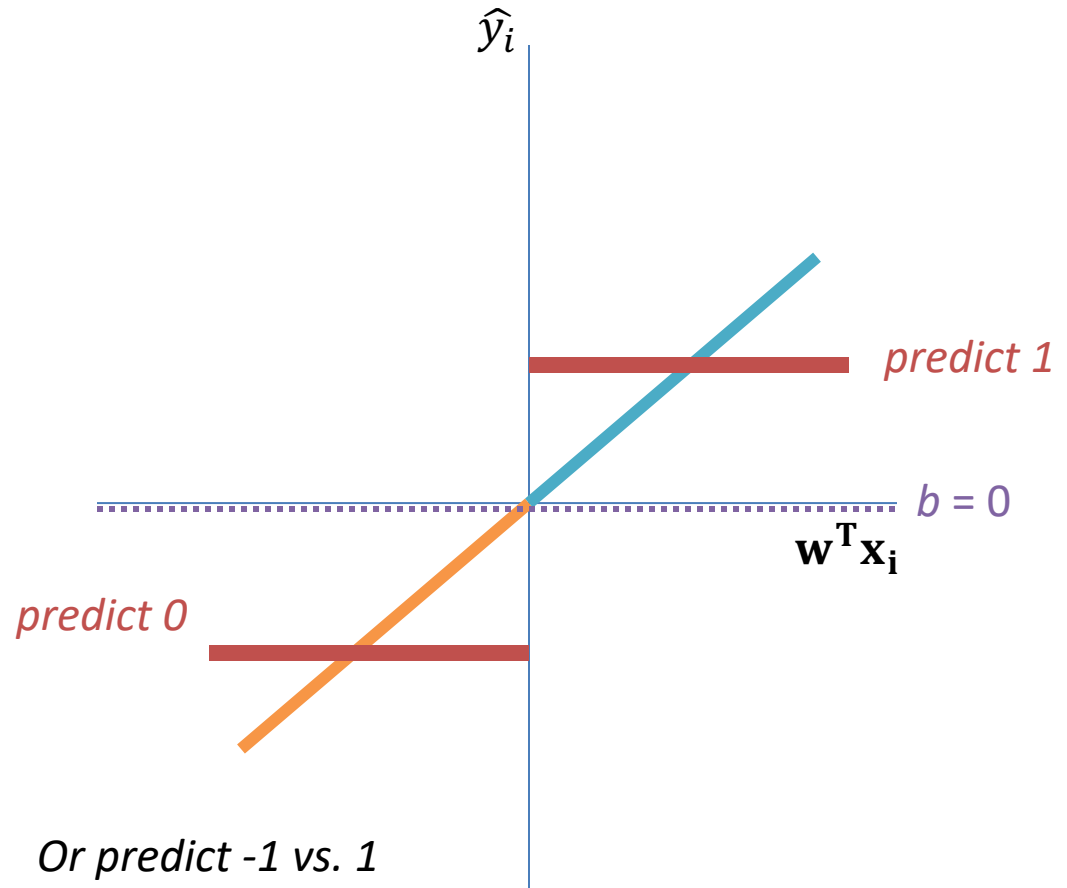
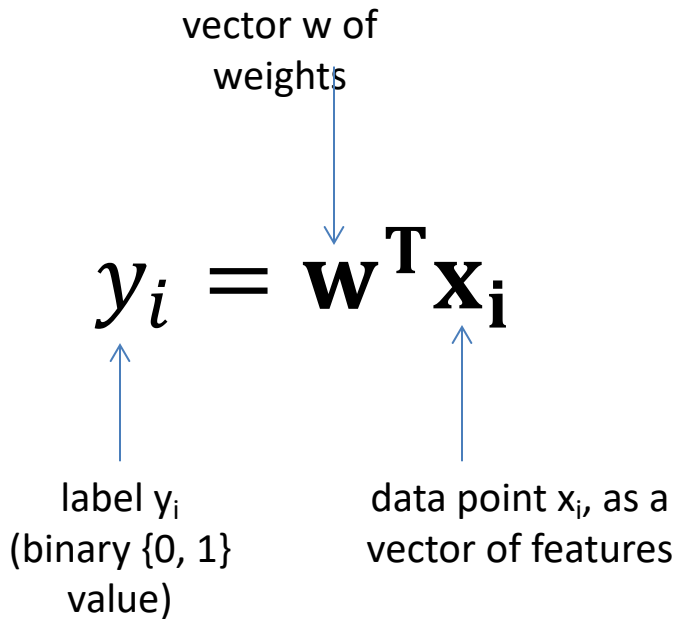


# Decision Rules



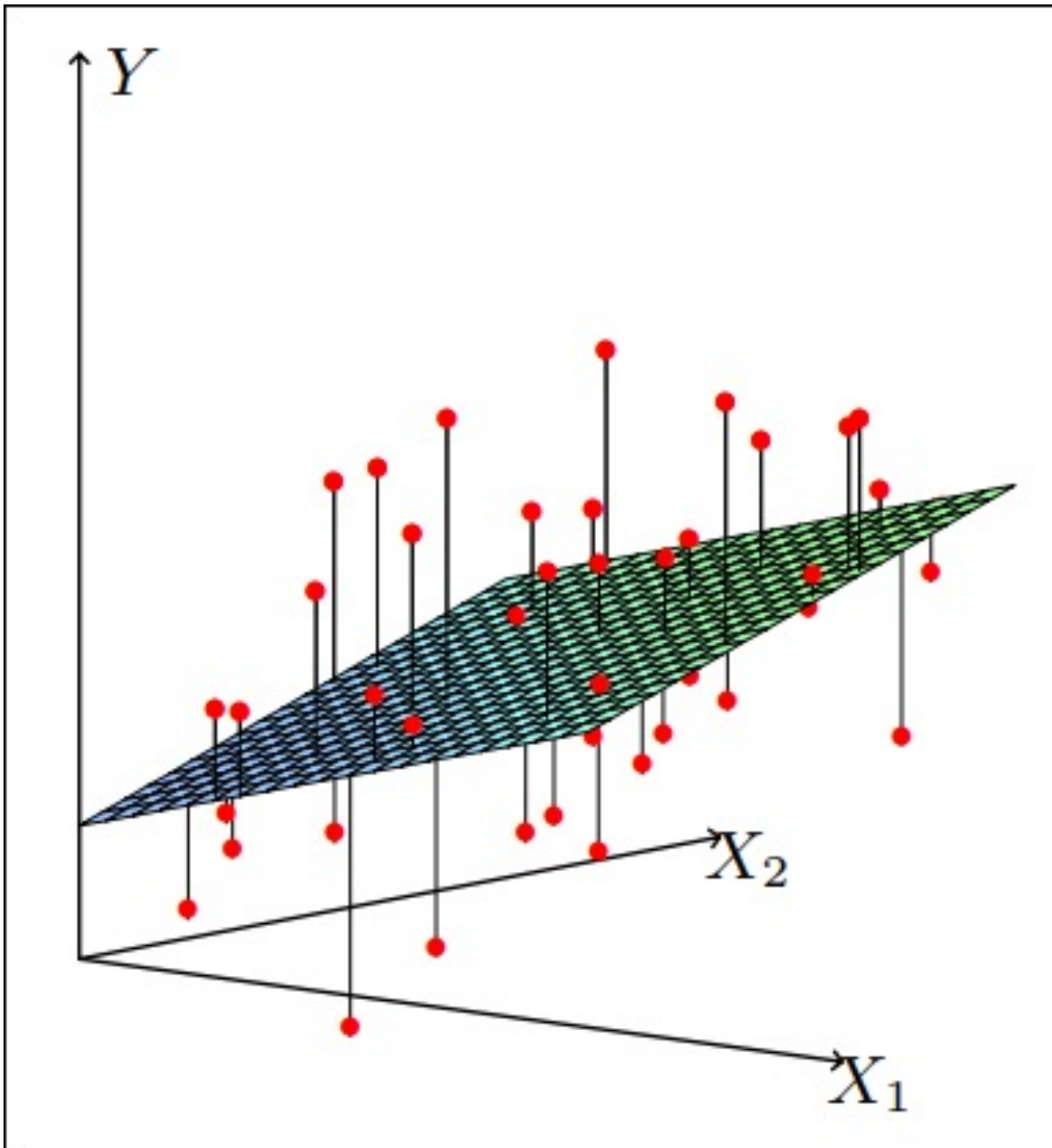
decision rule: 
$$\hat{y}_i = \begin{cases} 0, & \mathbf{w}^T \mathbf{x}_i < 0 \\ 1, & \mathbf{w}^T \mathbf{x}_i \geq 0 \end{cases}$$

# Decision Rules

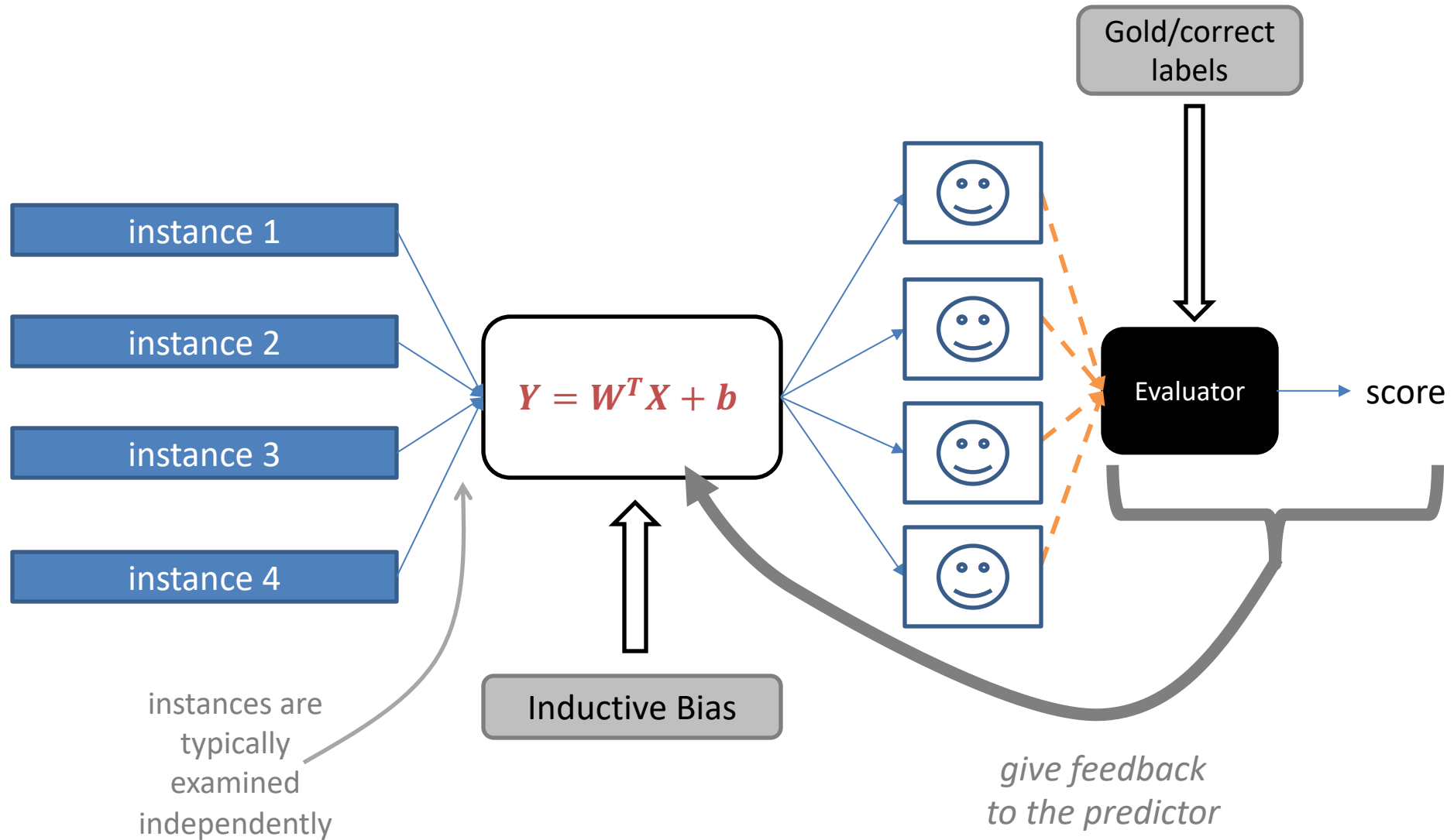


decision rule:  $\hat{y}_i = \begin{cases} -1, & \mathbf{w}^T \mathbf{x}_i < 0 \\ 1, & \mathbf{w}^T \mathbf{x}_i \geq 0 \end{cases}$

# Linear Models in Multiple Dimensions



# Linear Models in the Basic Framework



# Central Question: How Well Are We Doing?

Reminder!

The performance score does not have to be the same thing as the loss function you optimize

Classification

- Precision, Recall, F1
- Accuracy
- Log-loss
- ROC-AUC
- ...

Regression

- (Root) Mean Square Error
- Mean Absolute Error
- ...

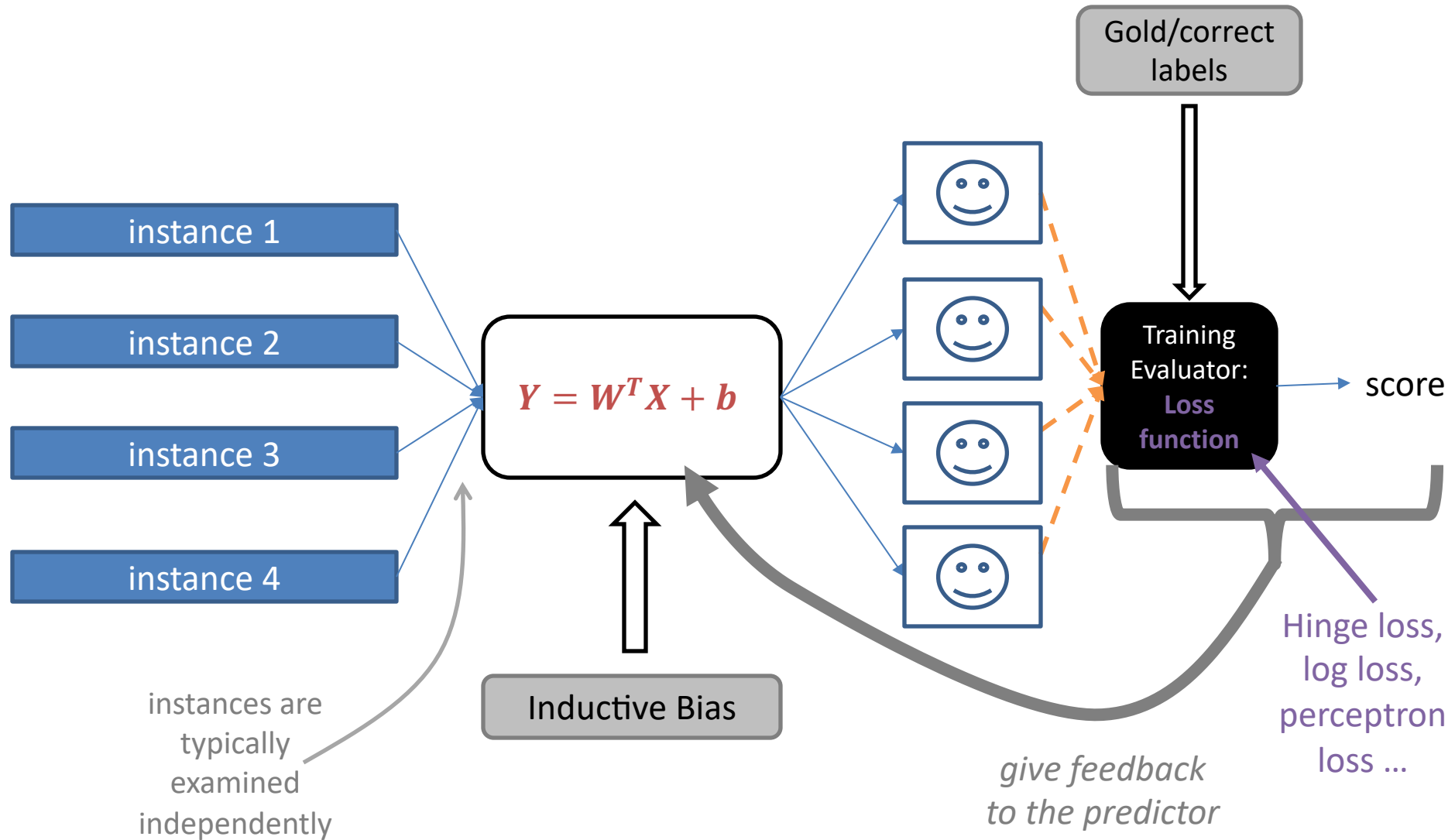
Clustering

- Mutual Information
- V-score
- ...

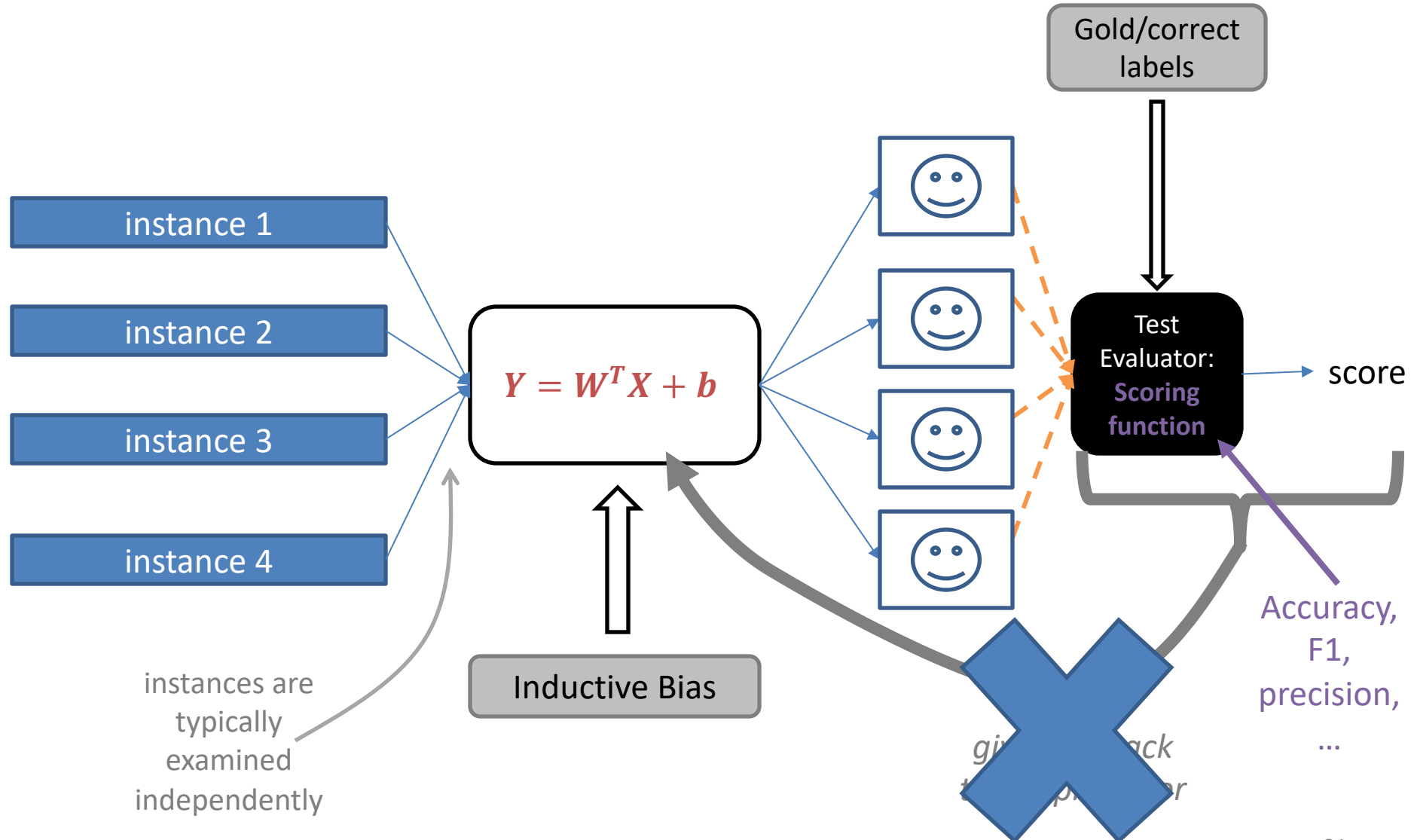
*the **task**: what kind of problem are you solving?*

# How do we **learn** these linear classification methods?

Change the loss function. (478/678 topics)



# How do we evaluate these linear classification methods? Change the eval function.



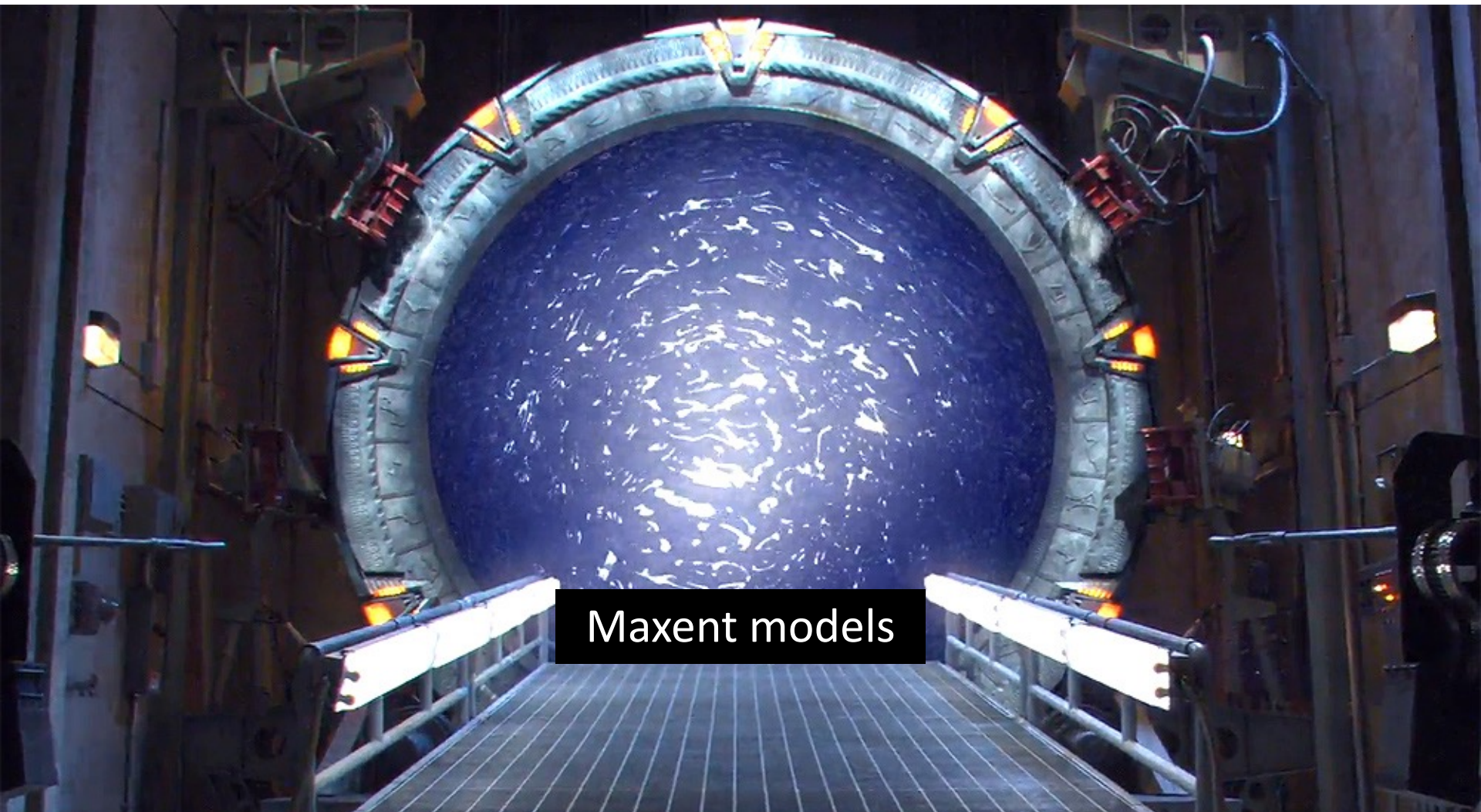


# What if

- We want a unified way to predict more than two classes?
- We want a probabilistic (bounded, interpretable) score?
- We want to use *transformations* of our data  $x$  to help make decisions?

## What if

- We want a unified way to predict more than two classes?
  - We want a probabilistic (bounded, interpretable) score?
- We want to use *transformations* of our data  $x$  to help make decisions?



Maxent models

# Terminology

common ML  
term

Log-Linear Models

as statistical  
regression

(Multinomial) logistic regression

Softmax regression

based in  
information theory

Maximum Entropy models (MaxEnt)

a form of

Generalized Linear Models

viewed as

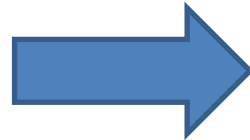
Discriminative Naïve Bayes

to be cool  
today :)

Very shallow (sigmoidal) neural nets

# Turning Scores into Probabilities

score( s: Michael Jordan, coach Phil Jackson and the star cast, including Scottie Pippen, took the Chicago Bulls to six National Basketball Association championships.  
h: The Bulls basketball team is based in Chicago. , ENTAILED ) > score( s: Michael Jordan, coach Phil Jackson and the star cast, including Scottie Pippen, took the Chicago Bulls to six National Basketball Association championships.  
h: The Bulls basketball team is based in Chicago. , NOT ENTAILED )



$p(\text{ENTAILED} \mid \text{s: Michael Jordan, coach Phil Jackson and the star cast, including Scottie Pippen, took the Chicago Bulls to six National Basketball Association championships.  
h: The Bulls basketball team is based in Chicago.}) > p(\text{NOT ENTAILED} \mid \text{s: Michael Jordan, coach Phil Jackson and the star cast, including Scottie Pippen, took the Chicago Bulls to six National Basketball Association championships.  
h: The Bulls basketball team is based in Chicago.})$



# Core Aspects to Maxent Classifier

## $p(y|x)$

- **features**  $f(x, y)$  between  $x$  and  $y$  that are meaningful;
- **weights**  $w$  (one per feature) to say how important each feature is; and
- a way to **form probabilities** from  $f$  and  $w$

$$p(y|x) = \frac{\exp(\mathbf{w}^T f(x, y))}{\sum_{y'} \exp(\mathbf{w}^T f(x, y'))}$$

# Discriminative Document Classification

s: Michael Jordan, coach Phil Jackson and the star cast, including Scottie Pippen, took the Chicago Bulls to six National Basketball Association championships.

**ENTAILED**

h: The Bulls basketball team is based in Chicago.

# Discriminative Document Classification

s: Michael Jordan, coach Phil Jackson and the star cast, including Scottie Pippen, took the **Chicago** Bulls to six National Basketball Association championships.

h: The Bulls basketball team is based in **Chicago**.

## ENTAILED

These extractions are all **features** that have **fired** (likely have some significance)

# Discriminative Document Classification

s: Michael Jordan, coach Phil Jackson and the star cast, including Scottie Pippen, took the **Chicago Bulls** to six National Basketball Association championships.

h: The **Bulls** basketball team is based in **Chicago**.

## ENTAILED

These extractions are all **features** that have **fired** (likely have some significance)



# Discriminative Document Classification

s: Michael Jordan, coach Phil Jackson and the star cast, including Scottie Pippen, took the **Chicago Bulls** to six National **Basketball** Association championships.

h: The Bulls **basketball** team is based in **Chicago**.

## ENTAILED

These extractions are all **features** that have **fired** (likely have some significance)

We need to *score* the different extracted clues.

s: Michael Jordan and Scottie Pippen, including Scottie Pippen, took the **Chicago Bulls** to six National **Basketball** Association championships.

score<sub>1</sub>(📄, ENTAILED)

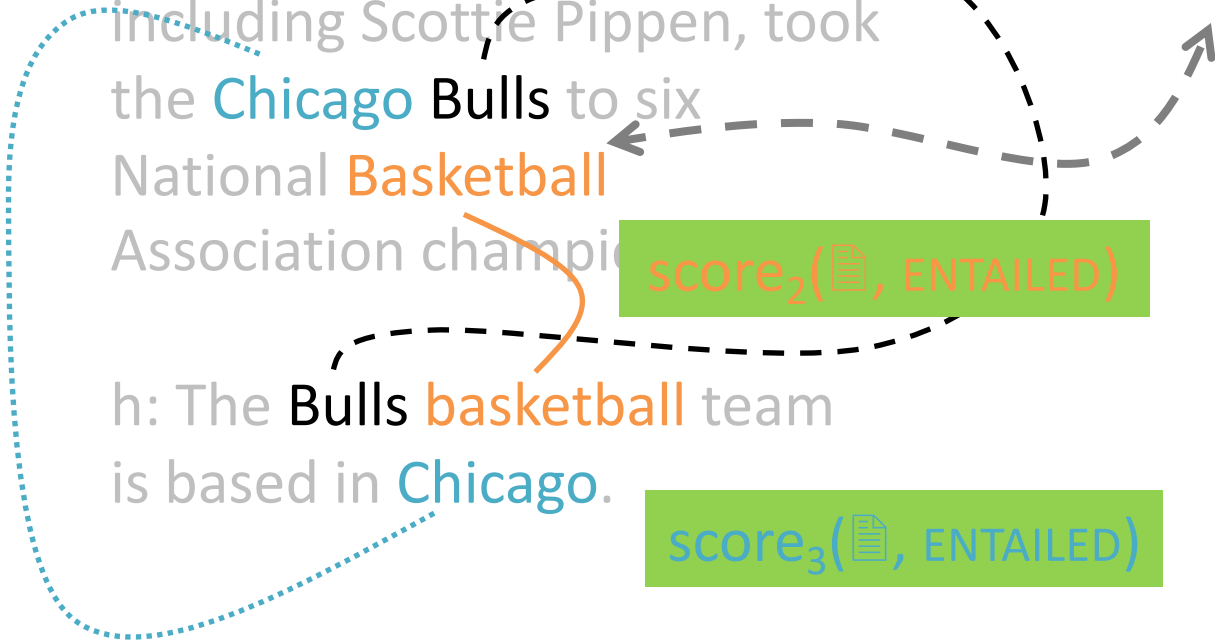
ENTAILED

h: The Bulls **basketball** team is based in **Chicago**.

score<sub>2</sub>(📄, ENTAILED)

h: The Bulls **basketball** team is based in **Chicago**.

score<sub>3</sub>(📄, ENTAILED)



# Score and Combine Our Clues

score<sub>1</sub>(📄, ENTAILED)

score<sub>2</sub>(📄, ENTAILED)

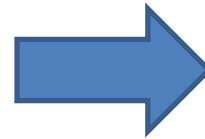
score<sub>3</sub>(📄, ENTAILED)

...

score<sub>k</sub>(📄, ENTAILED)

...

COMBINE



posterior  
probability of  
ENTAILED

# Scoring Our Clues

score ( s: Michael Jordan, coach Phil Jackson and the star cast, including Scottie Pippen, took the Chicago Bulls to six National Basketball Association championships.  
h: The Bulls basketball team is based in Chicago. , ENTAILED ) =

*(ignore the  
feature indexing  
for now)*

score<sub>1</sub>(📄, ENTAILED)

+

score<sub>2</sub>(📄, ENTAILED)

+

score<sub>3</sub>(📄, ENTAILED)

+

...

A linear  
scoring  
model!

# Scoring Our Clues

score ( s: Michael Jordan, coach Phil Jackson and the star cast, including Scottie Pippen, took the Chicago Bulls to six National Basketball Association championships.  
h: The Bulls basketball team is based in Chicago. , ENTAILED ) =

Learn these scores... but how?

What do we optimize?

score<sub>1</sub>(📄, ENTAILED)

score<sub>2</sub>(📄, ENTAILED)

score<sub>3</sub>(📄, ENTAILED)

...

+

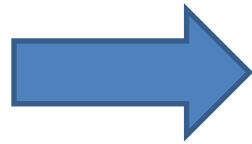
+

+

A linear scoring model!

# Turning Scores into Probabilities (More Generally)

$$\text{score}(x, y_1) > \text{score}(x, y_2)$$



$$p(y_1 | x) > p(y_2 | x)$$

KEY IDEA

# Maxent Modeling

$p(\text{ENTAILED} |$

**s:** Michael Jordan, coach Phil Jackson and the star cast, including Scottie Pippen, took the Chicago Bulls to six National Basketball Association championships.

**h:** The Bulls basketball team is based in Chicago.

$) \propto$

$\exp(\text{score}(\text{, ENTAILED}))$

**s:** Michael Jordan, coach Phil Jackson and the star cast, including Scottie Pippen, took the Chicago Bulls to six National Basketball Association championships.  
**h:** The Bulls basketball team is based in Chicago.

A linear scoring model!

# Maxent Modeling

$$p(\text{ENTAILED} \mid \begin{array}{l} \text{s: Michael Jordan, coach Phil} \\ \text{Jackson and the star cast,} \\ \text{including Scottie Pippen, took} \\ \text{the Chicago Bulls to six} \\ \text{National Basketball Association} \\ \text{championships.} \\ \text{h: The Bulls basketball team is} \\ \text{based in Chicago.} \end{array}) \propto \exp\left(\begin{array}{l} \text{score}_1(\text{document}, \text{ENTAILED}) \\ \text{score}_2(\text{document}, \text{ENTAILED}) \\ \text{score}_3(\text{document}, \text{ENTAILED}) \\ \dots \end{array} + \dots\right)$$



# Maxent Modeling

$$p(\text{ENTAILED} \mid \begin{array}{l} \text{s: Michael Jordan, coach Phil} \\ \text{Jackson and the star cast,} \\ \text{including Scottie Pippen, took} \\ \text{the Chicago Bulls to six} \\ \text{National Basketball Association} \\ \text{championships.} \\ \text{h: The Bulls basketball team is} \\ \text{based in Chicago.} \end{array}) \propto \exp(\begin{array}{l} \text{score}_1(\text{document}, \text{ENTAILED}) \\ \text{score}_2(\text{document}, \text{ENTAILED}) \\ \text{score}_3(\text{document}, \text{ENTAILED}) \\ \dots \end{array})$$

*Learn the scores (but we'll declare what combinations should be looked at)*

# Maxent Modeling

$p$ (

ENTAILED

|

s: Michael Jordan, coach Phil Jackson and the star cast, including Scottie Pippen, took the Chicago Bulls to six National Basketball Association championships.  
h: The Bulls basketball team is based in Chicago.

)  $\propto$

$\exp$ (

$\text{weight}_1 * \text{applies}_1(\text{📄}, \text{ENTAILED})$

$\text{weight}_2 * \text{applies}_2(\text{📄}, \text{ENTAILED})$

$\text{weight}_3 * \text{applies}_3(\text{📄}, \text{ENTAILED})$

...

+  
+  
+  
)  
)

# Maxent Modeling

$$p(\text{ENTAILED} \mid \text{...}) \propto$$

s: Michael Jordan, coach Phil Jackson and the star cast, including Scottie Pippen, took the Chicago Bulls to six National Basketball Association championships.

h: The Bulls basketball team is based in Chicago.

$$\exp\left(\begin{matrix} \text{weight}_1 * \text{applies}_1(\text{...}, \text{ENTAILED}) \\ \text{weight}_2 * \text{applies}_2(\text{...}, \text{ENTAILED}) \\ \text{weight}_3 * \text{applies}_3(\text{...}, \text{ENTAILED}) \\ \vdots \end{matrix}\right)$$

K different weights... for K different features

# Maxent Modeling

$$p(\text{ENTAILED} \mid \text{...}) \propto$$

s: Michael Jordan, coach Phil Jackson and the star cast, including Scottie Pippen, took the Chicago Bulls to six National Basketball Association championships.

h: The Bulls basketball team is based in Chicago.

$$\exp\left(\begin{array}{l} \text{weight}_1 * \text{applies}_1(\text{...}, \text{ENTAILED}) \\ \text{weight}_2 * \text{applies}_2(\text{...}, \text{ENTAILED}) \\ \text{weight}_3 * \text{applies}_3(\text{...}, \text{ENTAILED}) \\ \vdots \end{array}\right)$$

K different  
weights...

for K different  
features...

multiplied and  
then summed

# Maxent Modeling

$$p(\text{ENTAILED} \mid \text{document}) \propto$$

s: Michael Jordan, coach Phil Jackson and the star cast, including Scottie Pippen, took the Chicago Bulls to six National Basketball Association championships.

h: The Bulls basketball team is based in Chicago.

$$\exp(\text{Dot\_product of weight\_vec feature\_vec}(\text{document}, \text{ENTAILED}))$$

K different  
weights...

for K different  
features...

multiplied and  
then summed

# Maxent Modeling

$$p(\text{ENTAILED} \mid \text{ } ) \propto$$

s: Michael Jordan, coach Phil Jackson and the star cast, including Scottie Pippen, took the Chicago Bulls to six National Basketball Association championships.

h: The Bulls basketball team is based in Chicago.

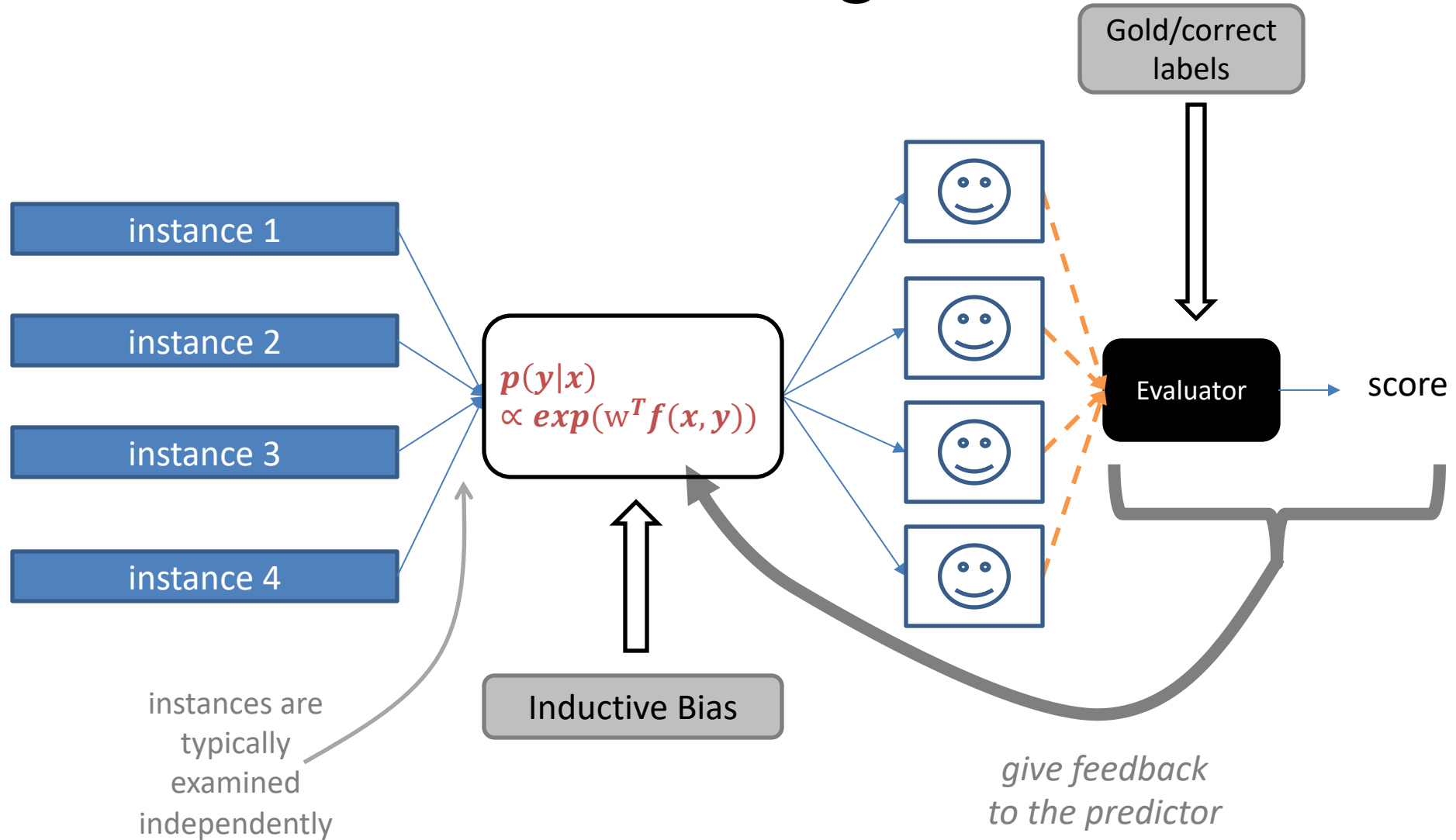
$$\exp( w^T f(\text{document}, \text{ENTAILED}) )$$

K different  
weights...

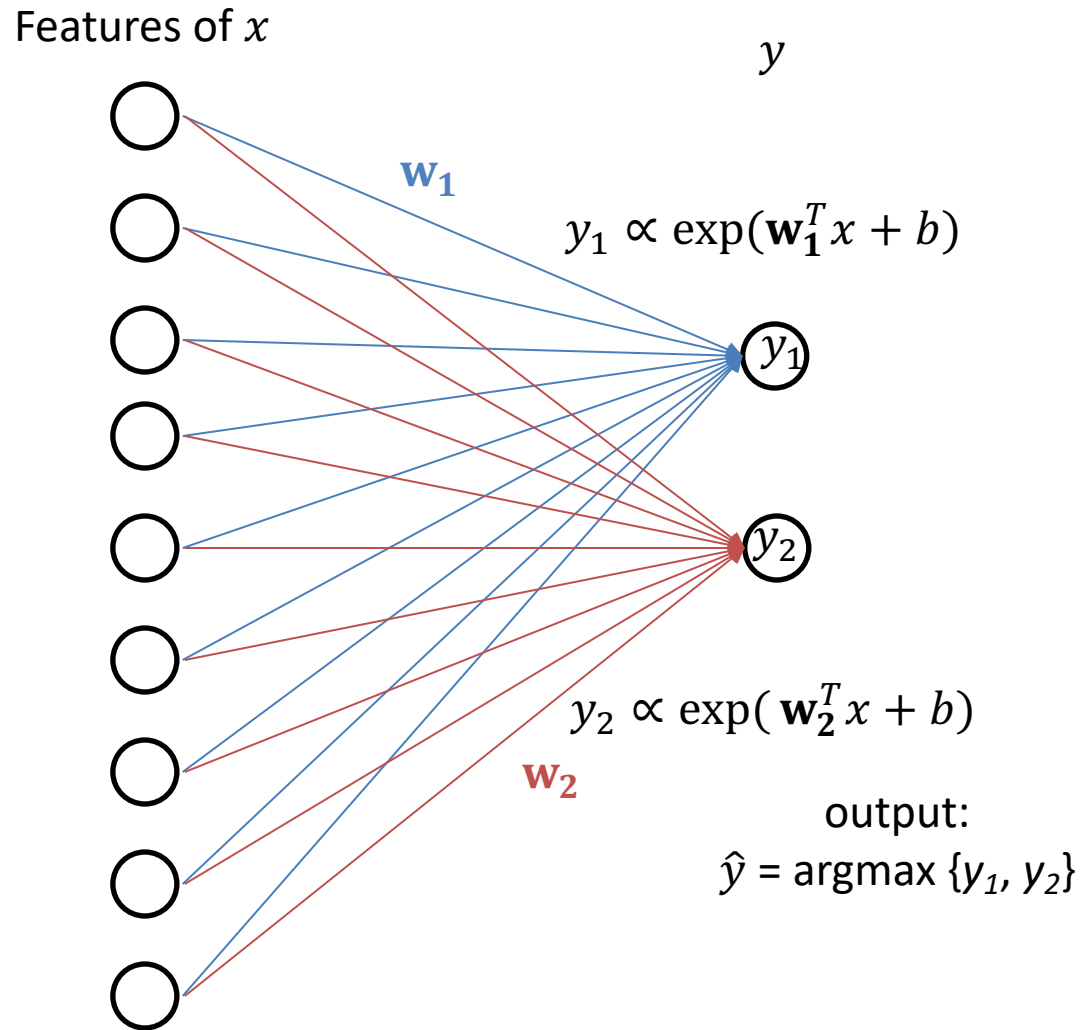
for K different  
features...

multiplied and  
then summed

# Machine Learning Framework: Learning

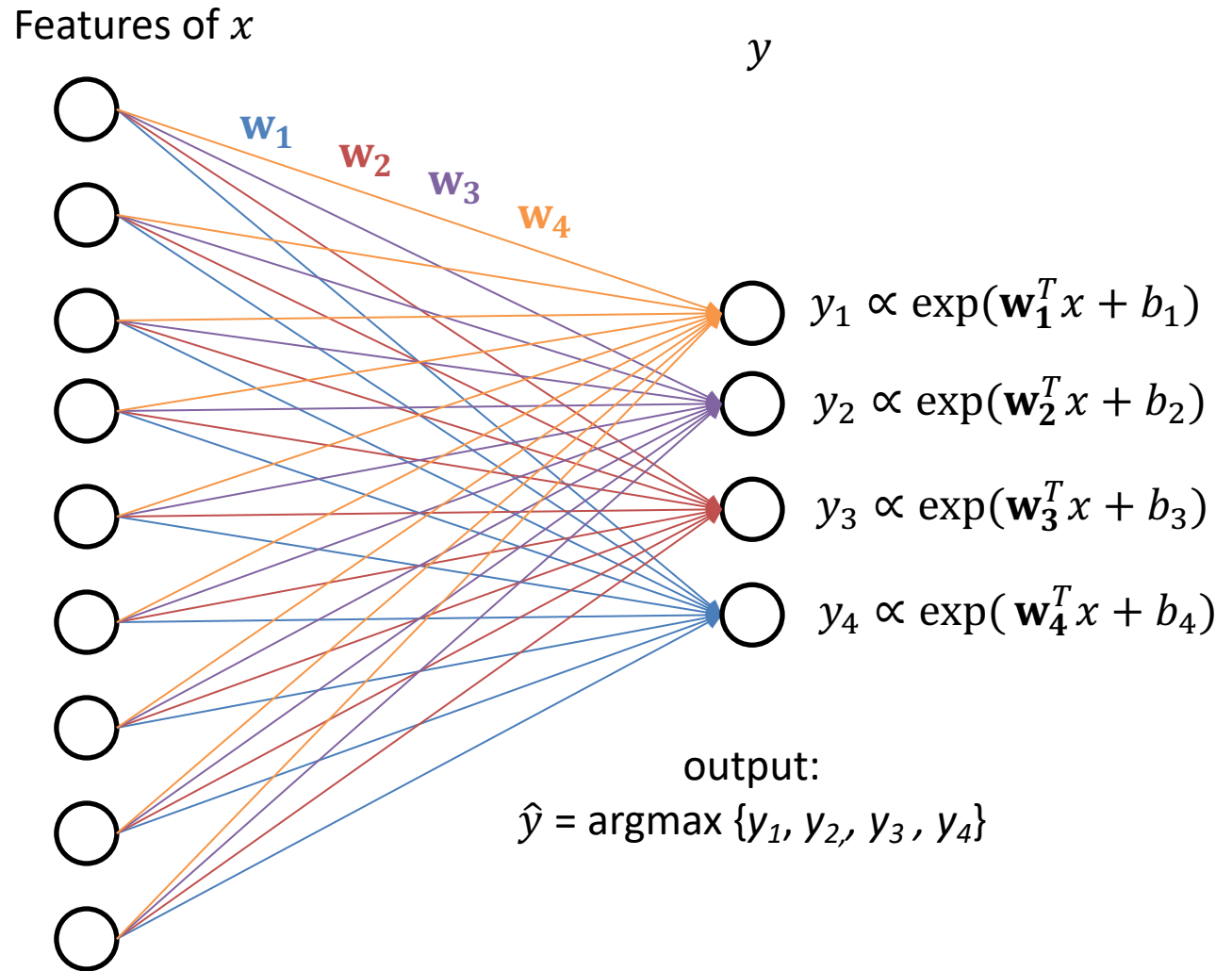


# A Graphical View of Logistic Regression/Classification (2 classes)





# A Graphical View of Logistic Regression/Classification (4 classes)



# sklearn.linear\_model.LogisticRegression ¶

```
class sklearn.linear_model.LogisticRegression(penalty='l2', *, dual=False, tol=0.0001, C=1.0, fit_intercept=True,
intercept_scaling=1, class_weight=None, random_state=None, solver='lbfgs', max_iter=100, multi_class='auto', verbose=0,
warm_start=False, n_jobs=None, l1_ratio=None)
```

[source]

Logistic Regression (aka logit, MaxEnt) classifier.

In the multiclass case, the training algorithm uses the one-vs-rest (OvR) scheme if the 'multi\_class' option is set to 'ovr', and uses the cross-entropy loss if the 'multi\_class' option is set to 'multinomial'. (Currently the 'multinomial' option is supported only by the 'lbfgs', 'sag', 'saga' and 'newton-cg' solvers.)

This class implements regularized logistic regression using the 'liblinear' library, 'newton-cg', 'sag', 'saga' and 'lbfgs' solvers. **Note that regularization is applied by default.** It can handle both dense and sparse input. Use C-ordered arrays or CSR matrices containing 64-bit floats for optimal performance; any other input format will be converted (and copied).

The 'newton-cg', 'sag', and 'lbfgs' solvers support only L2 regularization with primal formulation, or no regularization. The 'liblinear' solver supports both L1 and L2 regularization, with a dual formulation only for the L2 penalty. The Elastic-Net regularization is only supported by the 'saga' solver.

Read more in the [User Guide](#).

## Parameters:

**penalty** : {'l1', 'l2', 'elasticnet', 'none'}, default='l2'

Used to specify the norm used in the penalization. The 'newton-cg', 'sag' and 'lbfgs' solvers support only l2 penalties. 'elasticnet' is only supported by the 'saga' solver. If 'none' (not supported by the liblinear solver), no regularization is applied.

[https://scikit-learn.org/stable/modules/generated/sklearn.linear\\_model.LogisticRegression.html](https://scikit-learn.org/stable/modules/generated/sklearn.linear_model.LogisticRegression.html)