### CMSC 471: Machine Learning

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Some slides courtesy Tim Finin and Frank Ferraro

# Why study learning?

- **Discover** new things or structure previously unknown
  - Examples: data mining, scientific discovery
- Fill in skeletal or **incomplete specifications** in a domain
  - Large, complex systems can't be completely built by hand
     & require dynamic updating to incorporate new info.
  - Learning new characteristics expands the domain or expertise and lessens the "brittleness" of the system
- Acquire models automatically from data rather than by manual programming
- Build agents that can adapt to users, other agents, and their environment
- Understand and improve efficiency of human learning

#### What does it mean to learn?

Wesley has been taking an AI course

Geordi, the instructor, needs to determine if Wesley has "learned" the topics covered, at the end of the course

What is a "reasonable" exam?
(Bad) Choice 1: History of pottery
Wesley's performance is not indicative of what was learned in AI
(Bad) Choice 2: Questions answered during lectures
Open book?

A good test should test ability to answer "related" but "new" questions on the exam

#### Generalization

#### Model, parameters and hyperparameters

#### Model: mathematical formulation of system (e.g., classifier)

# Parameters: primary "knobs" of the model that are set by a learning algorithm



#### Hyperparameter: secondary "knobs" set by designer

http://www.uiparade.com/wp-content/uploads/2012/01/ui-design-pure-css.jpg



# score( Instance of data ("datum")





#### Machine Learning Framework: Learning



#### Machine Learning Framework: Learning







#### **Classify with Goodness**

# predicted label

= arg max label score(example, label)







Classifier (trained **model**)



Classifier
(trained
model)









What do we know *before* we see the data, and how does that influence our modeling decisions?

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Partition these into two groups...

What do we know *before* we see the data, and how does that influence our modeling decisions?



Partition these into two groups

Who selected red vs. blue?

What do we know *before* we see the data, and how does that influence our modeling decisions?



What do we know *before* we see the data, and how does that influence our modeling decisions?



#### AI & ML

## AI and Learning Today

- 50s&60s: neural network learning popular
   Marvin Minsky did neural networks for his dissertation
- Mid 60s: replaced by paradigm of manually encoding & using symbolic knowledge
   Cf. <u>Perceptrons</u>, Minsky & Papert book showed limitations of

perceptron model of neural networks

- 90s: more data & Web drove interest in statistical machine learning techniques & data mining
- Now: machine learning techniques & big data play biggest driver in almost all successful AI systems

... and neural networks are the current favorite approach



#### Neural Networks 1960

A man adjusting the random wiring network between the light sensors and association unit of scientist Frank Rosenblatt's Perceptron, or MARK 1 computer, at the Cornell Aeronautical Laboratory, Buffalo, New York, circa 1960. The machine is designed to use a type of artificial neural network, known as a perceptron.



#### Neural Networks 2020

Google's AIY Vision Kit (\$89.99 at Target) is an intelligent camera that can recognize objects, detect faces and emotions. Download and use a variety of image recognition neural networks to customize the Vision Kit for your own creation. Included in the box: Raspberry Pi Zero WH, Pi Camera V2, Micro SD Card, Micro USB Cable, Push Button.

Currently \$58.85 on Amazon

#### Machine Learning Successes

- Games: chess, go, poker
- Text sentiment analysis
- Email spam detection
- Recommender systems (e.g., Netflix, Amazon)
- Machine translation
- Speech understanding
- SIRI, Alexa, Google Assistant, ...

- Autonomous vehicles
- Individual face recognition
- Understanding digital images
- Credit card fraud detection
- Showing annoying ads

## The Big Idea and Terminology

Given some data, learn a model of how the world works that lets you predict new data

- Training Set: Data from which you learn initially
- Model: What you learn; a "model" of how inputs are associated with outputs
- Test set: New data you test your model against
- **Corpus:** A body of text data (pl.: corpora)
- Representation: The computational expression of data

#### Major Machine learning paradigms (1)

- **Rote**: 1-1 mapping from inputs to stored representation, learning by memorization, association-based storage & retrieval
- Induction: Use specific examples to reach general conclusions
- Clustering: Unsupervised discovery of natural groups in data

#### Major Machine learning paradigms (2)

- Analogy: Find correspondence between different representations
- **Discovery**: Unsupervised, specific goal not given
- Genetic algorithms: Evolutionary search techniques, based on survival of the fittest
- **Reinforcement:** Feedback (positive or negative reward) given at the end of a sequence of steps
- **Deep learning:** *artificial neural networks* with *representation learning* for ML tasks

#### **CORE TERMINOLOGY**

#### Three Axes for Thinking About Your ML Problem

Classification	Fully-supervised	Probabilistic Neural
Regression	Semi-supervised	Generative Memory- based
		Conditional Exemplar
Clustering	Un-supervised	Spectral …
the task: what kind	the data: amount of	the approach: how

the task: what kind of problem are you solving? the **data**: amount of human input/number of labeled examples the **approach**: how any data are being used 32

# Types of learning problems

- **Supervised**: learn from training examples
  - Regression:
  - Classification: Decision Trees, SVM
- Unsupervised: learn w/o training examples
  - Clustering
  - Dimensionality reduction
  - Word embeddings
- Reinforcement learning: improve performance using feedback from actions taken
- Lots more we won't cover
  - Hidden Markov models, Learning to rank, Semi-supervised learning, Active learning ...
## **Machine Learning Problems**

_	Supervised Learning	Unsupervised Learning
Discrete	classification or categorization	clustering
Continuous	regression	dimensionality reduction

## Supervised learning

- Given training examples of inputs & corresponding outputs, produce "correct" outputs for new inputs
- Two important scenarios:
  - -**Classification:** outputs typically labels (goodRisk, badRisk); learn decision boundary to separate classes
- -Regression: aka *curve fitting* or *function approximation*; Learn a *continuous* input-output mapping from examples, e.g., for a zip code, predict house sale price given its square footage

## **Unsupervised Learning**

Given only *unlabeled* data as input, learn some sort of structure, e.g.:

- **Clustering**: group Facebook friends based on similarity of post texts and friends
- **Embeddings**: Find sets of words whose meanings are related (e.g., doctor, hospital)
- **Topic modelling**: Induce N topics and words most common in documents about each

## Inductive Learning Framework

- Raw input data from sensors or a database preprocessed to obtain feature vector, X, of relevant features for classifying examples
- Each **X** is a list of (attribute, value) pairs
- *n* attributes (a.k.a. features): fixed, positive, and finite
- Features have fixed, finite number # of possible values
   Or continuous within some well-defined space, e.g., "age"
- Each example is a point in an *n*-dimensional feature space
  - X = [Person:Sue, EyeColor:Brown, Age:Young, Sex:Female]
  - X = [Cheese:f, Sauce:t, Bread:t]
  - X = [Texture:Fuzzy, Ears:Pointy, Purrs:Yes, Legs:4]

## Inductive Learning Framework Example



#### **Classification Examples**

. . .

Assigning subject categories, topics, or genres

Spam detection

Authorship identification

Age/gender identification Language Identification Sentiment analysis

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Input: an instance a fixed set of classes  $C = \{c_1, c_2, ..., c_J\}$ 

. . .

Output: a predicted class c from C

## Classification: Hand-coded Rules?

Assigning subject categories, topics, or genres

Spam detection

Age/gender identification Language Identification Sentiment analysis

Authorship identification

Rules based on combinations of words or other features spam: black-list-address OR ("dollars" AND "have been selected")

. . .

Accuracy can be high If rules carefully refined by expert

Building and maintaining these rules is expensive

Can humans faithfully assign uncertainty?

## Classification: Supervised Machine Learning

. . .

Assigning subject categories, topics, or genres

Spam detection

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#### Input:

an instance da fixed set of classes  $C = \{c_1, c_2, ..., c_J\}$ A training set of m hand-labeled instances  $(d_1, c_1), ..., (d_m, c_m)$ 

Output:

a learned classifier  $\ensuremath{\nu}$  that maps instances to classes

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a learned classifier  $\ensuremath{\nu}$  that maps instances to classes

y learns to associate certain *features* of instances with their labels

## Classification: Supervised Machine Learning

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Output:

a learned classifier  $\gamma$  that maps instances to classes

Naïve Bayes Logistic regression Support-vector machines k-Nearest Neighbors

## Classification Example: Face Recognition



#### What is a good *representation* for images?

Pixel values? Edges?

Courtesy from Hamed Pirsiavash

#### Classification Example: Sequence & Structured Prediction

Image: Spanish French Hindi - detectedImage: Spanish ArabicTranslateImage: Spanish French Hindi - detectedImage: Spanish ArabicTranslateMittgZjcArui Åt üscAn ut the spanish ArabicImage: Spanish ArabicTranslateMittgZjcArui Åt üscAn ut the spanish ArabicImage: Spanish ArabicImage: Spanish ArabicImage: Spanish ArabicMittgZjcArui Åt üscAn ut the spanish ArabicImage: Spanish ArabicImage: Spanish ArabicImage: Spanish ArabicMittgZjcArui Åt üscAn ut the spanish AttabicImage: Spanish ArabicImage: Spanish ArabicImage: Spanish ArabicMittgZjcArui Åt üscAn ut the spanish AttabicImage: Spanish ArabicImage: Spanish ArabicImage: Spanish ArabicMittgZjcArui Åt üscAn ut the spanish AttabicImage: Spanish ArabicImage: Spanish ArabicImage: Spanish ArabicImage: Spanish ArabicMittgZjcArui Åt üscAn ut the spanish AttabicImage: Spanish ArabicImage: Spanish ArabicImage: Spanish ArabicImage: Spanish ArabicImage: Spanish ArabicMittgZjcArui Åt üscAn ut the Spanish AttabicImage: Spanish ArabicImage: Spanish ArabicImage: Spanish ArabicImage: Spanish ArabicImage: Spanish ArabicMittgZjcArui Åt UscAn ut the Spanish AttabicImage: Spanish ArabicImage: Spanish Arabic<	Google	+Subhransu 🏭 🚺 🕂 🎇
EnglishSpanishFrenchHindi - detectedऑस्ट्रेलिया में खेली जा रही त्रिकोणीय एकदिवसीय अंतरराष्ट्रीय क्रिकेट मैचों की सिरीज़ में रविवार का दिन सुपर संडे साबित हो सकता है.Translateमंजवान ऑस्ट्रेलिया और भारत मेलवर्न में आमने-सामने होंगे. इसके पहले मुकाबले में ऑस्ट्रेलिया ने इंग्लैंड को तीन विकेट से हराकर बोनस अंक से साथ शानवार शुरुआत की.शारत इस एकदिवसीय सिरीज से पहले ऑस्ट्रेलिया के हाथों चार टेस्ट मैचों की सिरीज में 0-2 से हारा था. तीसरे टेस्ट मैच के ड्रा सामप्त होने के बाद भारत के कप्तान महेंद्र सिंह धोनी ने टेस्ट क्रिकेट से संन्यास का एलान भी कर दिया था. अब टेस्ट क्रिकेट के सफ़ेब कपड़े ना सही वनडे की रंगीन जर्मी में धोनी अपना जलवा विषाने के विये बेचैन होंगे.अब टेस्ट क्रिकेट के सफ़ेब कपड़े ना सही वनडे की रंगीन वर्मी में धोनी अपना जलवा विषाने के विये बेचैन होंगे.	Translate	
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	अंतरराष्ट्रीय क्रिकेट मैचों की सिरीज़ में रविवार का दिन सुपर संडे साबित हो सकता हैं. मेजबान ऑस्ट्रेलिया और भारत मेलबर्न में आमने-सामने होंगे. इसके पहले मुक्राबले में ऑस्ट्रेलिया ने इंग्लैंड को तीन विकेट से हराकर बोनस अंक से साथ शानदार शुरुआत की. भारत इस एकदिवसीय सिरीज़ से पहले ऑस्ट्रेलिया के हाथों चार टेस्ट मैचों की सिरीज़ में 0-2 से हारा था. तीसरे टेस्ट मैच के ड्रा समाप्त होने के बाद भारत के कप्तान महेंद्र सिंह धोनी ने टेस्ट क्रिकेट से संन्यास का एलान भी कर दिया था. अब टेस्ट क्रिकेट के सफ़ेद कपड़े ना सही वनडे की रंगीन नर्जी में की याना उन्हा किलाने के जिसे केने- रोंगे	<ul> <li>international cricket match can be a Sunday Super Sunday.</li> <li>Australia and India will face each host in Melbourne. The first match Australia beat England by three wickets with a superb debut of bonus points.</li> <li>The hands of the one-day series in India before Australia lost 0-2 in the four-Test series.</li> <li>After the end of the third Test draw India captain Mahendra Singh Dhoni was also announced his retirement from Test cricket. Now is not the right day of Test cricket whites Dhoni color jersey will be anxious to show his usual self.</li> <li></li></ul>





Inject your knowledge into a learning system

Feature representation

Training data: labeled examples

Model

**Courtesy Hamed Pirsiavash** 

Inject your knowledge into a learning system

Problem specific

Difficult to learn from bad ones

Feature representation

Training data: labeled examples

Model

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Inject your knowledge into a learning system

Problem specific	Labeling data == \$\$\$
Difficult to learn from bad ones	Sometimes data is available for "free"

Feature representation

Training data: labeled examples

Model

Inject your knowledge into a learning system

		No single learning algorithm
Problem specific	Labeling data == \$\$\$	is always good ("no free
		lunch")
Difficult to learn from bad	Sometimes data is	
ones	available for "free"	Different learning
		algorithms work differently

Feature representation

Training data: labeled examples

Model

1 1

• • •

1

#### Regression

#### Like classification, but real-valued

#### Regression Example: Stock Market Prediction

S&P 500 S&P Indices: .INX - Jan 16 4:30 PM ET

#### 2,019.42 +26.75 (1.34%)



#### **Unsupervised learning: Clustering**



#### LINEAR MODELS

#### Linear Models



- Can be used for either regression or classification
- A number of instances for classification. Common ones are:
  - Perceptron
  - Linear SVM
  - Logistic regression
    - (yes, even though "regression" is in the name ☺)

#### Linear Models: Core Idea



Model the relationship between the input data X and corresponding labels Y via a linear relationship (non-zero intercepts *b* are okay)

$$Y = W^T X + b$$

Items to learn: W, b

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$$Y = W^T X + b$$

Items to learn: W, b

For classification: one class is on one side of this line, the other class is on the other

#### 1.1. Linear Models

1.1.1. Ordinary Least Squares 1.1.2. Ridge regression and classification 1.1.3. Lasso 1.1.4. Multi-task Lasso 1.1.5. Elastic-Net 1.1.6. Multi-task Elastic-Net 1.1.7. Least Angle Regression 1.1.8. LARS Lasso 1.1.9. Orthogonal Matching Pursuit (OMP) 1.1.10. Bayesian Regression 1.1.11. Logistic regression 1.1.12. Generalized Linear Regression 1.1.13. Stochastic Gradient Descent - SGD 1.1.14. Perceptron 1.1.15. Passive Aggressive Algorithms 1.1.16. Robustness regression: outliers and modeling errors 1.1.17. Polynomial regression: extending linear models with basis functions

# Linear Models in sklearn

These all have easy-to-use interfaces, with the same core interface:

- Training: model.fit(X=training features, y=training labels)
- Prediction: model.predict(X=eval\_features)

#### https://scikit-learn.org/stable/modules/linear\_model.html

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#### LINEAR

CLASS torch.nn.Linear(in\_features, out\_features, bias=True)

Applies a linear transformation to the incoming data:  $y=xA^T+b$ 

This module supports TensorFloat32.

#### Variables

- ~Linear.weight the learnable weights of the module of shape (out\_features, in\_features). The values are initialized from  $\mathcal{U}(-\sqrt{k},\sqrt{k})$ , where  $k = \frac{1}{\text{in_features}}$
- ~Linear.bias the learnable bias of the module of shape (out\_features). If bias is True, the values are initialized from  $\mathcal{U}(-\sqrt{k},\sqrt{k})$  where  $k = \frac{1}{\text{in features}}$

Examples:

>>> m = nn.Linear(20, 30)
>>> input = torch.randn(128, 20)
>>> output = m(input)
>>> print(output.size())
torch.Size([128, 30])

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#### https://pytorch.org/docs/stable/generated/torch.nn.Linear.html

## Linear Models in pytorch

These are "building blocks" not full models.

#### A Simple Linear Model

# predict $y_i$ from $\mathbf{x_i}$ value $y_i$

data point x<sub>i</sub>, as a vector of features

#### A Graphical View of Linear Models



#### A Simple Linear Model for Regression



#### A Simple Linear Model for Regression



#### A Simple Linear Model for Regression



#### A Simple Linear Model for Classification




### A Simple Linear Model for Classification











Linear Models in Multiple Dimensions

### Linear Models in the Basic Framework





#### How do we learn these linear classification methods? Change the loss function. (478/678 topics)



## How do we evaluate these linear classification methods? Change the eval function.



### What if

 We want a unified way to predict more than two classes?

## • We want a probabilistic (bounded, interpretable) score?

 We want to use *transformations* of our data x to help make decisions?

#### What if

- We want a unified way to predict more than two classes?
- We want a probabilistic (bounded, interpretable) score?
- We want to use *transformations* of our data x to help make decisions?



### Terminology

common ML term	Log-Linear Models
as statistical regression	(Multinomial) logistic regression
	Softmax regression
based in information theory	Maximum Entropy models (MaxEnt)
a form of	Generalized Linear Models
viewed as	Discriminative Naïve Bayes
to be cool today :)	Very shallow (sigmoidal) neural nets

### **Turning Scores into Probabilities**



### Core Aspects to Maxent Classifier p(y|x)

- features f(x, y) between x and y that are meaningful;
- weights  $\theta$  (one per feature) to say how important each feature is; and
- a way to form probabilities from f and  $\theta$

 $\exp(\theta^T f(x,y))$ p(y|x) = $\overline{\sum_{v'} \exp(\theta^T f(x, y'))}$ 

s: Michael Jordan, coach Phil Jackson and the star cast, including Scottie Pippen, took the Chicago Bulls to six National Basketball Association championships.

h: The Bulls basketball team is based in Chicago.

#### **ENTAILED**

s: Michael Jordan, coach Phil Jackson and the star cast, including Scottie Pippen, took the Chicago Bulls to six National Basketball Association championships.

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#### **ENTAILED**

These extractions are all **features** that have **fired** (likely have some significance)

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\*\*\*\*\*

#### **ENTAILED**

These extractions are all **features** that have **fired** (likely have some significance)

## We need to *score* the different extracted clues.



### Score and Combine Our Clues

score<sub>1</sub>( $\square$ , ENTAILED) score<sub>2</sub>( $\square$ , ENTAILED) score<sub>3</sub>( $\square$ , ENTAILED)



posterior probability of ENTAILED

```
...
score<sub>k</sub>(圕, ENTAILED)
...
```

### **Scoring Our Clues**

### score

s: Michael Jordan, coach Phil Jackson and the star cast, including Scottie Pippen, took the Chicago Bulls to six National Basketball Association championships.
h: The Bulls basketball team is based in Chicago.

, ENTAILED) =

(ignore the feature indexing for now) score<sub>1</sub>(, ENTAILED) score<sub>2</sub>(, ENTAILED) score<sub>3</sub>(, ENTAILED)



### **Scoring Our Clues**

### score

s: Michael Jordan, coach Phil Jackson and the star cast, including Scottie Pippen, took the Chicago Bulls to six National Basketball Association championships.
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, ENTAILED) =

Learn these scores... but how?

What do we optimize?

score<sub>1</sub>( $\square$ , ENTAILED) score<sub>2</sub>( $\square$ , ENTAILED) score<sub>3</sub>( $\square$ , ENTAILED)



A linear scoring model! Turning Scores into Probabilities (More Generally)

# $score(x, y_1) > score(x, y_2)$

## $p(y_1|x) > p(y_2|x)$

**KEY IDEA** 

# p( ENTAILED

s: Michael Jordan, coach Phil Jackson and the star cast, including Scottie Pippen, took the Chicago Bulls to six National Basketball Association championships.
h: The Bulls basketball team is based in Chicago.

 $) \propto$ 

# exp(score (

s: Michael Jordan, coach Phil
Jackson and the star cast, including
Scottie Pippen, took the Chicago
Bulls to six National Basketball
Association championships.
h: The Bulls basketball team is based
in Chicago.



A linear scoring model!

# p( ENTAILED

s: Michael Jordan, coach Phil Jackson and the star cast, including Scottie Pippen, took the Chicago Bulls to six National Basketball Association championships.
h: The Bulls basketball team is based in Chicago.

 $) \propto$ 

exp(

score<sub>1</sub>( $\square$ , ENTAILED) score<sub>2</sub>( $\square$ , ENTAILED) score<sub>3</sub>( $\square$ , ENTAILED)

# p( ENTAILED

s: Michael Jordan, coach Phil Jackson and the star cast, including Scottie Pippen, took the Chicago Bulls to six National Basketball Association championships.
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 $) \propto$ 

exp(

score<sub>1</sub>( $\square$ , ENTAILED) score<sub>2</sub>( $\square$ , ENTAILED) score<sub>3</sub>( $\square$ , ENTAILED)

Learn the scores (but we'll declare what combinations should be looked at)

# p( ENTAILED

s: Michael Jordan, coach Phil Jackson and the star cast, including Scottie Pippen, took the Chicago Bulls to six National Basketball Association championships. h: The Bulls basketball team is based in Chicago.

 $) \propto$ 

weight<sub>1</sub> \* applies<sub>1</sub>( $\square$ , ENTAILED) weight<sub>2</sub> \* applies<sub>2</sub>( $\square$ , ENTAILED) weight<sub>3</sub> \* applies<sub>3</sub>( $\square$ , ENTAILED)

# exp(

s: Michael Jordan, coach Phil Jackson and the star cast, including Scottie Pippen, took **ENTAILED** the Chicago Bulls to six National Basketball Association championships. championships. h: The Bulls basketball team is based in Chicago.

exp( weight<sub>1</sub> \* applies<sub>1</sub>( $\square$ , ENTAILED) weight<sub>2</sub> \* applies<sub>2</sub>( $\square$ , ENTAILED) weight<sub>3</sub> \* applies<sub>3</sub>( $\square$ , ENTAILED) K different for K different weights... features

# p( ENTAILED

S: Michael Jordan, coach Phil Jackson and the star cast, including Scottie Pippen, took the Chicago Bulls to six National Basketball Association championships.
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 $) \propto$ 

weight<sub>1</sub> \* applies<sub>1</sub>(), ENTAILED)
exp(
weight<sub>2</sub> \* applies<sub>2</sub>(), ENTAILED)
weight<sub>3</sub> \* applies<sub>3</sub>(), ENTAILED
K different
weights...
for K different
features...

**\***))

multiplied and then summed

# p( ENTAILED

s: Michael Jordan, coach Phil
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 $)\propto$ 

**EXD Dot\_product of weight\_vec feature\_vec(B, ENTAILED)** 

K differentfor K differentweights...features...

multiplied and then summed

# p( ENTAILED

s: Michael Jordan, coach Phil
Jackson and the star cast,
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the Chicago Bulls to six
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championships.
h: The Bulls basketball team is
based in Chicago.

 $)\propto$ 

## $exp(\ \theta^T f(\mathbb{B}, \text{ENTAILED})$

K different for K different weights...

multiplied and then summed



## A Graphical View of Logistic Regression/Classification (2 classes)



## A Graphical View of Logistic Regression/Classification (4 classes)



#### sklearn.linear\_model.LogisticRegression¶

class sklearn.linear\_model.LogisticRegression(penalty='l2', \*, dual=False, tol=0.0001, C=1.0, fit\_intercept=True, intercept\_scaling=1, class\_weight=None, random\_state=None, solver='lbfgs', max\_iter=100, multi\_class='auto', verbose=0, warm\_start=False, n\_jobs=None, l1\_ratio=None)

Logistic Regression (aka logit, MaxEnt) classifier.

In the multiclass case, the training algorithm uses the one-vs-rest (OvR) scheme if the 'multi\_class' option is set to 'ovr', and uses the cross-entropy loss if the 'multi\_class' option is set to 'multinomial'. (Currently the 'multinomial' option is supported only by the 'lbfgs', 'sag', 'saga' and 'newton-cg' solvers.)

This class implements regularized logistic regression using the 'liblinear' library, 'newton-cg', 'sag', 'saga' and 'lbfgs' solvers. **Note that regularization is applied by default**. It can handle both dense and sparse input. Use C-ordered arrays or CSR matrices containing 64-bit floats for optimal performance; any other input format will be converted (and copied).

The 'newton-cg', 'sag', and 'lbfgs' solvers support only L2 regularization with primal formulation, or no regularization. The 'liblinear' solver supports both L1 and L2 regularization, with a dual formulation only for the L2 penalty. The Elastic-Net regularization is only supported by the 'saga' solver.

Read more in the User Guide.

## Parameters: penalty : {'l1', 'l2', 'elasticnet', 'none'}, default='l2' Used to specify the norm used in the penalization. The 'newton-cg', 'sag' and 'lbfgs' solvers support only l2 penalties. 'elasticnet' is only supported by the 'saga' solver. If 'none' (not supported by the liblinear solver), no regularization is applied.

https://scikit-

#### learn.org/stable/modules/generated/sklearn.linear\_model.LogisticRegression.html